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# Nuclear structure functions

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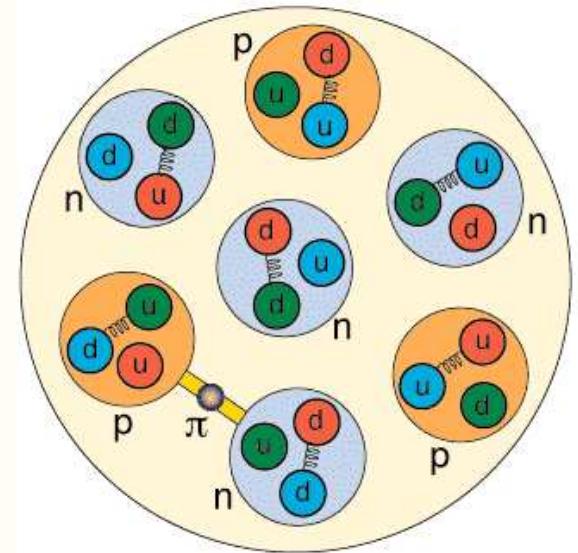
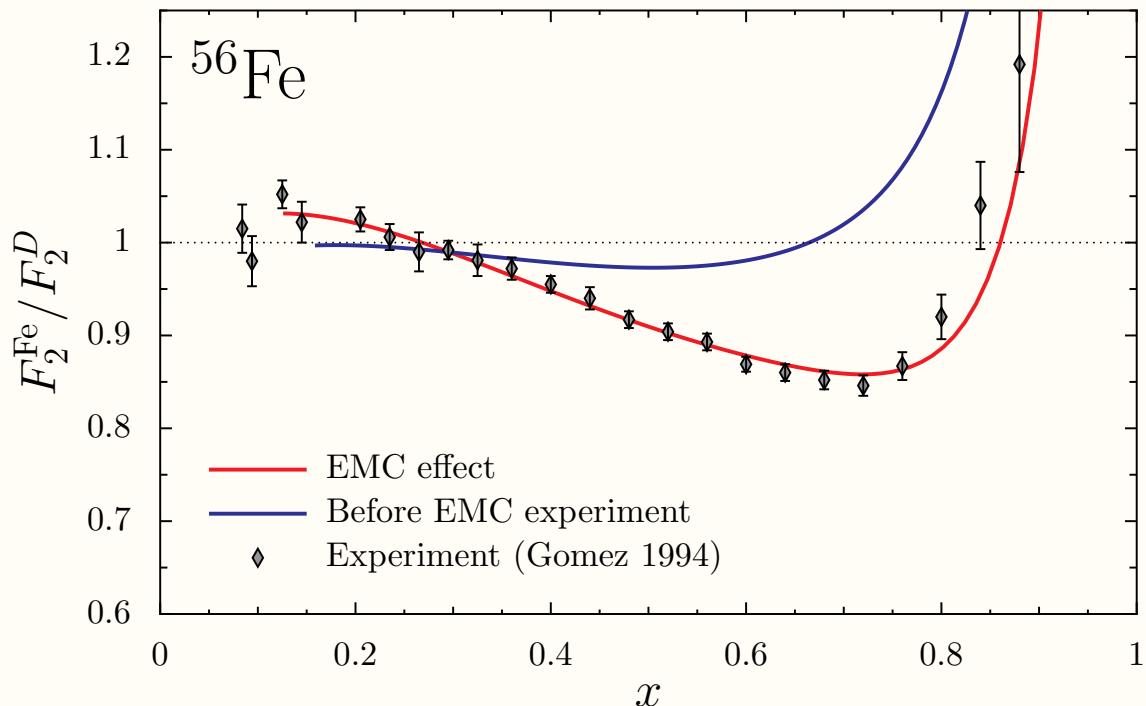
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(Adelaide University)

EIC Electroweak Workshop  
William & Mary 17–18 May 2010

# Theme

- Aspects of DIS on nuclear targets  $\Rightarrow$  nuclear structure functions
  - ◆ Highlight opportunities provided by nuclear systems to study QCD
  - ◆ Gain insight into nuclear structure from a QCD viewpoint
- Present complementary approach to traditional nuclear physics
  - ◆ formulated as a covariant quark theory
  - ◆ grounded in good description of mesons and baryons
  - ◆ at finite density self-consistent mean-field approach
  - ◆ bound nucleons differ from free nucleons
- Possible answers to many long standing questions: we address
  - ◆ EMC effect & NuTeV anomaly
- Highlight the unique opportunities provided by PV DIS on nuclei

# EMC Effect



- J. J. Aubert *et al.* [European Muon Collaboration], Phys. Lett. B **123**, 275 (1983).
- Immediate parton model interpretation:
  - ◆ valence quarks in nucleus carry less momentum than in nucleon
- Nuclear effects seem to influence the quarks in the bound nucleons
- What is the mechanism? After 25 years no consensus
- EMC  $\implies$  medium modification

# Medium Modification

- 50 years of traditional nuclear physics tells us that the nucleus is composed of nucleon-like objects
- However if a nucleon property is not protected by a symmetry its value may change in medium – for example:
  - ◆ mass, magnetic moment, size
  - ◆ quark distributions, form factors, GPDs, etc
- There must be medium modification:
  - ◆ nucleon propagator is changed in medium
  - ◆ off-shell effects ( $p^2 \neq M^2$ )
  - ◆ Lorentz covariance implies bound nucleon has 12 EM form factors

$$\langle J^\mu \rangle = \sum_{\alpha, \beta=+,-} \Lambda^\alpha(p') \left[ \gamma^\mu f_1^{\alpha\beta} + \frac{1}{2M} i\sigma^{\mu\nu} q_\nu f_2^{\alpha\beta} + q^\mu f_3^{\alpha\beta} \right] \Lambda^\beta(p)$$

- Need to understand these effects as first step toward QCD based understanding of nuclei

# Medium Modification

- 50 years of traditional nuclear physics tells us that the nucleus is composed of nucleon-like objects
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  - ◆ nucleon propagator is changed in medium
  - ◆ off-shell effects ( $p^2 \neq M^2$ )
  - ◆ **Becomes 2 form factors for on-shell nucleon**

$$\langle J^\mu \rangle = \bar{u}(p') [ \gamma^\mu F_1(Q^2) + \frac{1}{2M} i \sigma^{\mu\nu} q_\nu F_2(Q^2) ] u(p)$$

- Need to understand these effects as first step toward QCD based understanding of nuclei

# DIS on Nuclear Targets

- Why nuclear targets?
  - ◆ only targets with  $J \geq 1$  are nuclei
  - ◆ study QCD and nucleon structure at finite density
- Hadronic Tensor: in Bjorken limit & Callen-Gross ( $F_2 = 2x F_1$ )
  - ◆ For  $J = \frac{1}{2}$  target

$$W_{\mu\nu} = \left( g_{\mu\nu} \frac{p \cdot q}{q^2} + \frac{p_\mu p_\nu}{p \cdot q} \right) F_2(x, Q^2) + \frac{i\varepsilon_{\mu\nu\lambda\sigma} q^\lambda p^\sigma}{p \cdot q} g_1(x, Q^2)$$

- ◆ For arbitrary  $J$ :  $-J \leq H \leq J$  [2J+1 structure functions]

$$W_{\mu\nu}^H = \left( g_{\mu\nu} \frac{p \cdot q}{q^2} + \frac{p_\mu p_\nu}{p \cdot q} \right) F_{2A}^H(x_A, Q^2) + \frac{i\varepsilon_{\mu\nu\lambda\sigma} q^\lambda p^\sigma}{p \cdot q} g_{1A}^H(x_A, Q^2)$$

- Parton model expressions [2J+1 quark distributions]

$$F_{2A}^H(x_A) = \sum_q e_q^2 x_A [q_A^H(x_A) + \bar{q}_A^H(x_A)] ; \quad \text{parity} \implies F_{2A}^H = F_{2A}^{-H}$$

# DIS on Nuclear Targets

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$$F_{2A}(x) = \frac{1}{2J+1} \sum_{H=-J}^J F_{2A}^H(x)$$

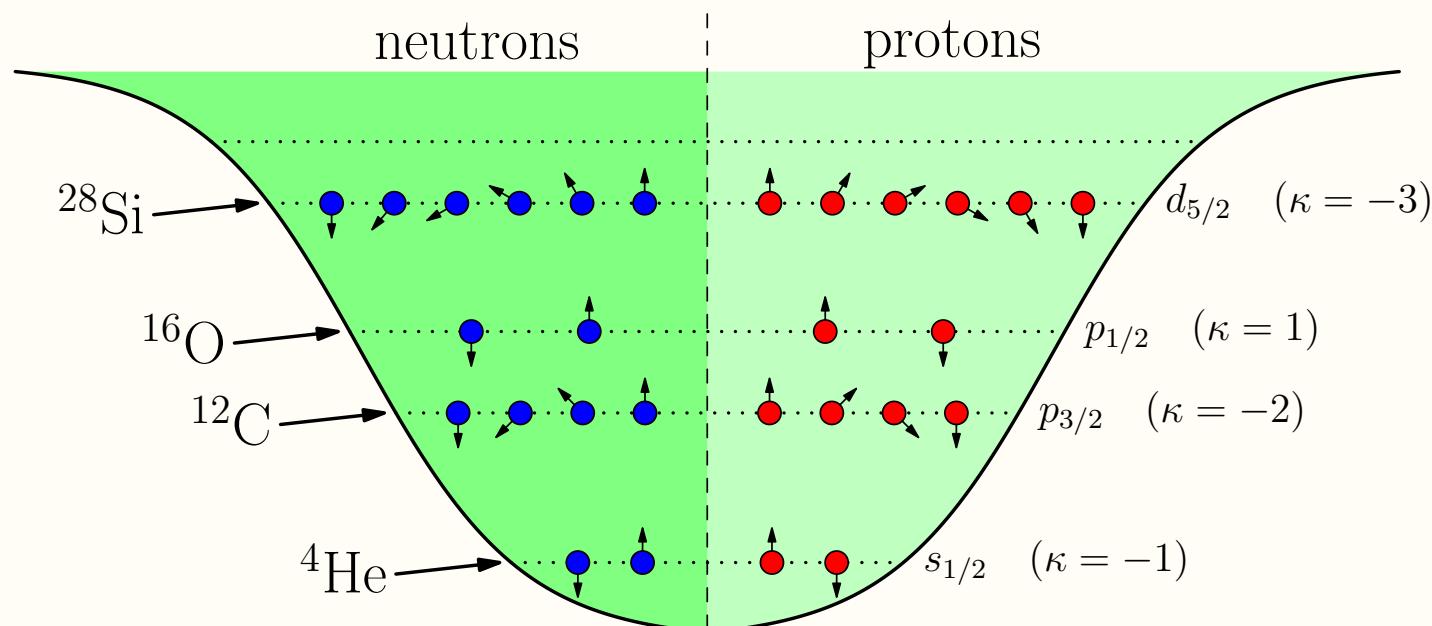
# Finite nuclei quark distributions

- Definition of finite nuclei quark distributions

$$q_A^H(x_A) = \frac{P^+}{A} \int \frac{d\xi^-}{2\pi} e^{iP^+ x_A \xi^- / A} \langle A, P, H | \bar{\psi}_q(0) \gamma^+ \psi_q(\xi^-) | A, P, H \rangle$$

- Approximate using a modified convolution formalism

$$q_A^H(x_A) = \sum_{\alpha, \kappa, m} \int dy_A \int dx \delta(x_A - y_A x) f_{\alpha, \kappa, m}^{(H)}(y_A) q_{\alpha, \kappa}(x)$$



# Finite nuclei quark distributions

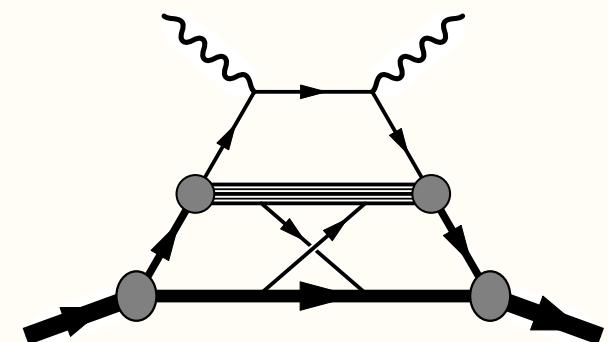
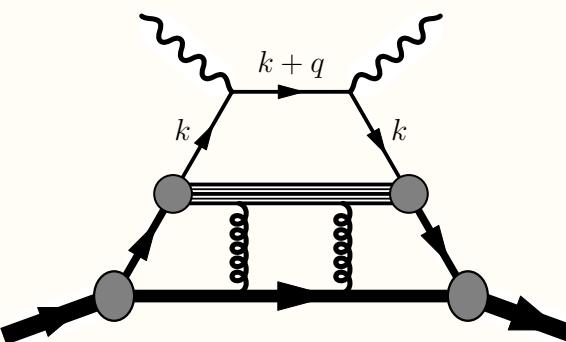
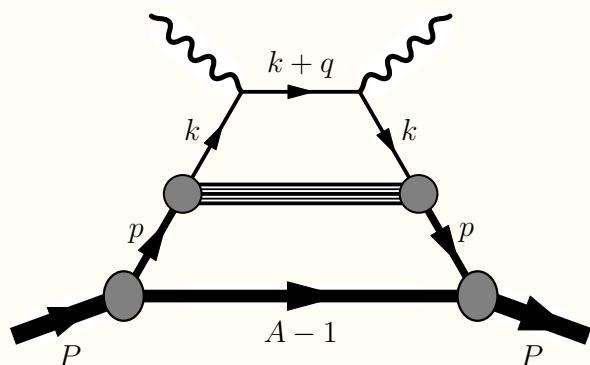
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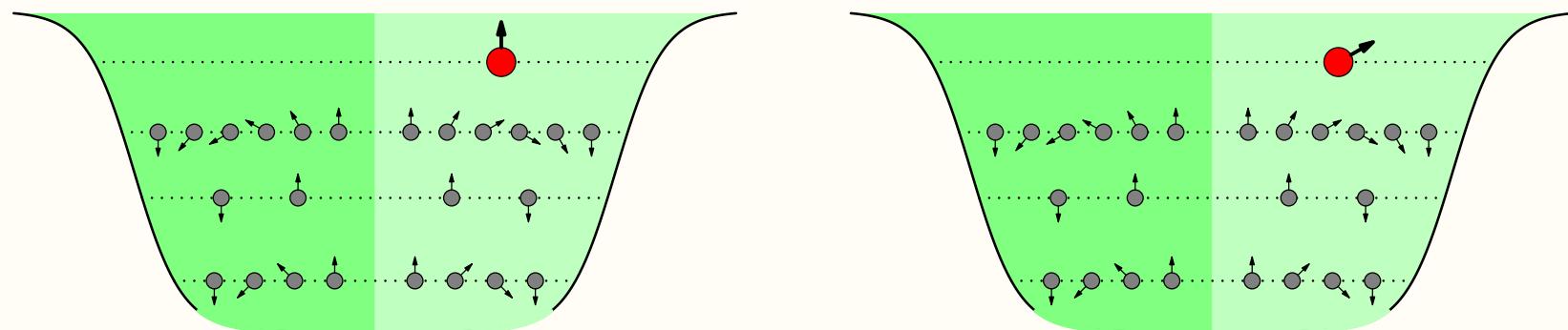
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- Convolution formalism diagrammatically:

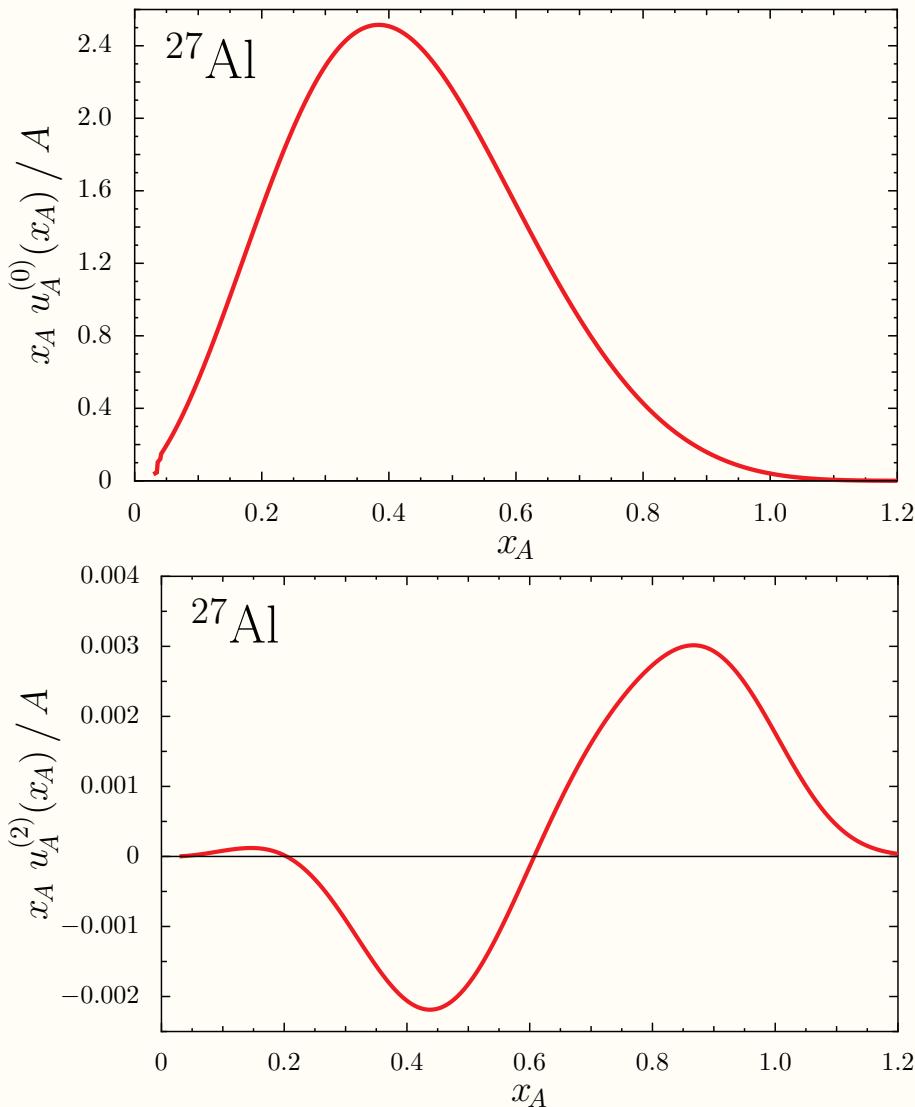


# Convolution Formalism: implications



- Assume all spin is carried by the valence nucleons
  - ◆ If  $A \gtrsim 8$  and for example if:  $J = \frac{3}{2} \implies F_{2A}^{3/2} \simeq F_{2A}^{1/2}$
- This is a model independent result within the convolution formalism
- Introduce multipole quark distributions
$$q^{(K)}(x) \equiv \sum_H (-1)^{J-H} \sqrt{2K+1} \begin{pmatrix} J & J & K \\ H & -H & 0 \end{pmatrix} q^H(x), \quad K = 0, 2, \dots, 2J$$
- Example:  $J = \frac{3}{2} \longrightarrow q^{(0)} = q^{\frac{3}{2}} + q^{\frac{1}{2}} \quad q^{(2)} = q^{\frac{3}{2}} - q^{\frac{1}{2}}$
- Higher multipoles encapsulate difference between helicity distributions

# Some multipole quark distributions result



- Large  $K > 1$  multipole PDFs would be very surprising
  - ◆  $\implies$  large off-shell effects &/or non-nucleon components, etc

# New Sum Rules

- Sum rules for multipole quark distributions

$$\int dx x^{n-1} q^{(K)}(x) = 0, \quad K, n \text{ even}, \quad 2 \leq n < K,$$
$$\int dx x^{n-1} \Delta q^{(K)}(x) = 0, \quad K, n \text{ odd}, \quad 1 \leq n < K.$$

- Examples:

$$J = \frac{3}{2} \implies \langle \Delta q^{(3)}(x) \rangle = 0$$

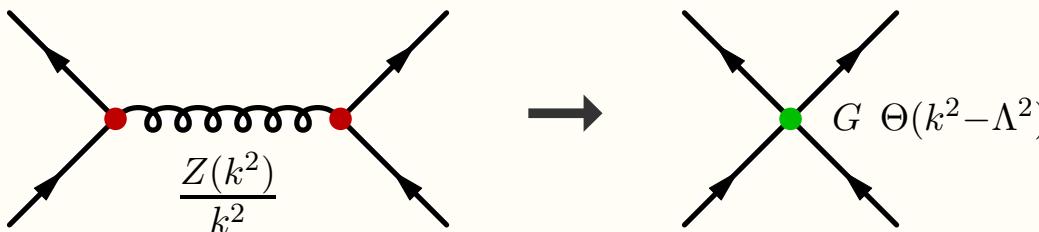
$$J = 2 \implies \langle \Delta q^{(3)}(x) \rangle = \langle q^{(4)}(x) \rangle = 0$$

$$J = \frac{5}{2} \implies \langle \Delta q^{(3)}(x) \rangle = \langle q^{(4)}(x) \rangle = \langle \Delta q^{(5)}(x) \rangle = \langle x^2 \Delta q^{(5)}(x) \rangle = 0$$

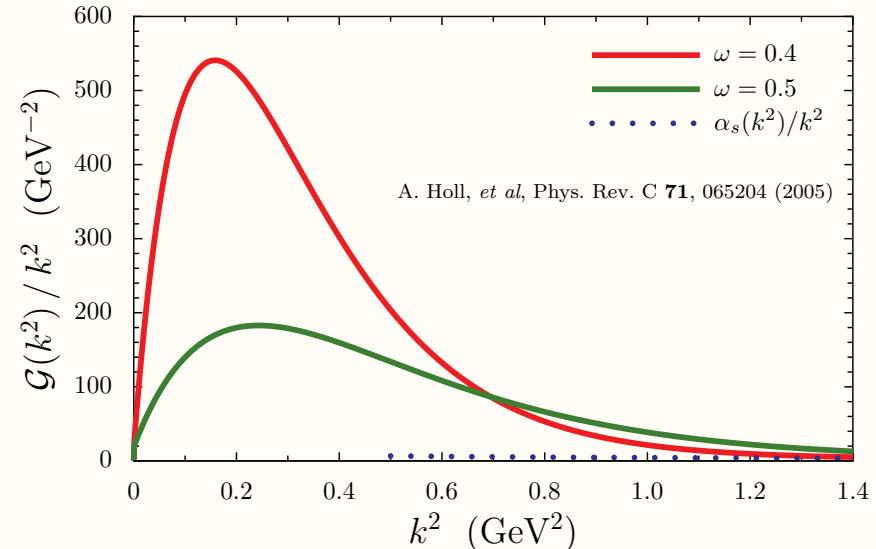
- Sum rules place tight constraints on multipole PDFs
- Jaffe and Manohar, *DIS from arbitrary spin targets*, Nucl. Phys. B **321**, 343 (1989).

# Nambu–Jona-Lasinio Model

- Interpreted as low energy chiral effective theory of QCD



- Can be motivated by infrared enhancement of gluon propagator  
e.g. DSEs and Lattice QCD

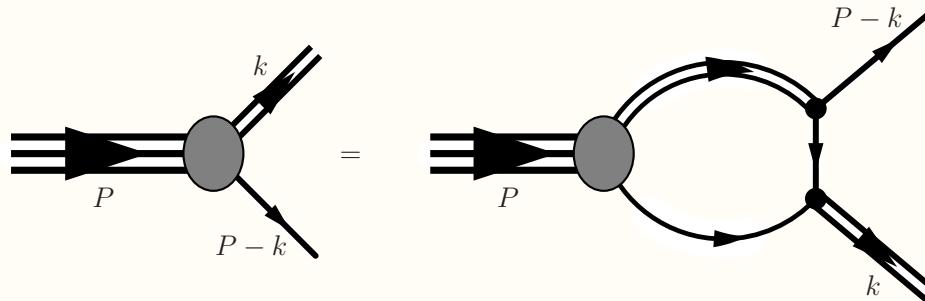


- Investigate the role of quark degrees of freedom.
- NJL has same symmetries as QCD
- Lagrangian:

$$\mathcal{L}_{NJL} = \bar{\psi} (i\cancel{\partial} - m) \psi + G (\bar{\psi} \Gamma \psi)^2$$

# Nucleon in the NJL model

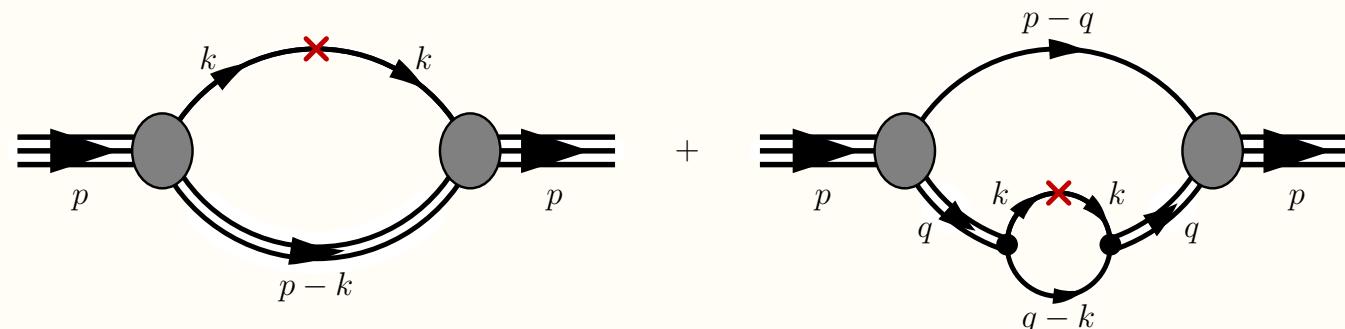
- Nucleon approximated as quark-diquark bound state
- Use relativistic Faddeev approach:



- Nucleon quark distributions

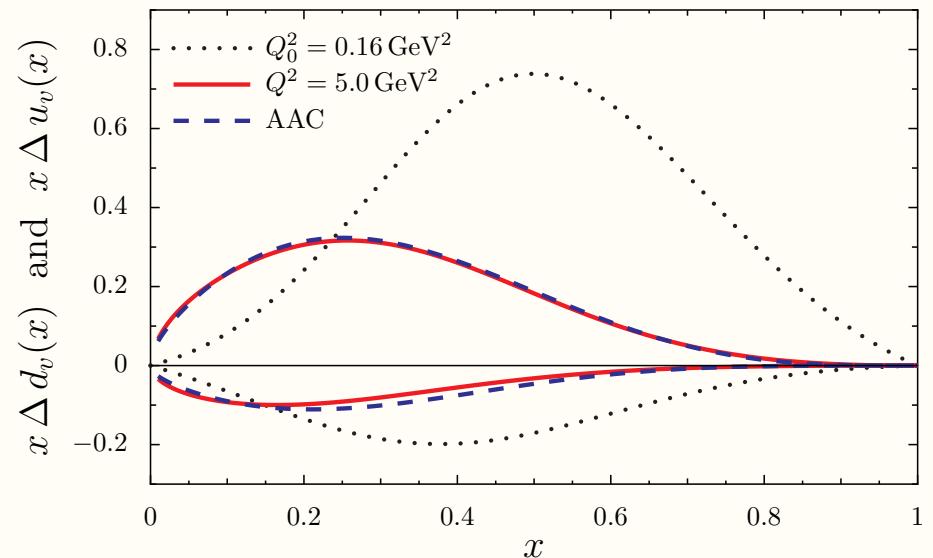
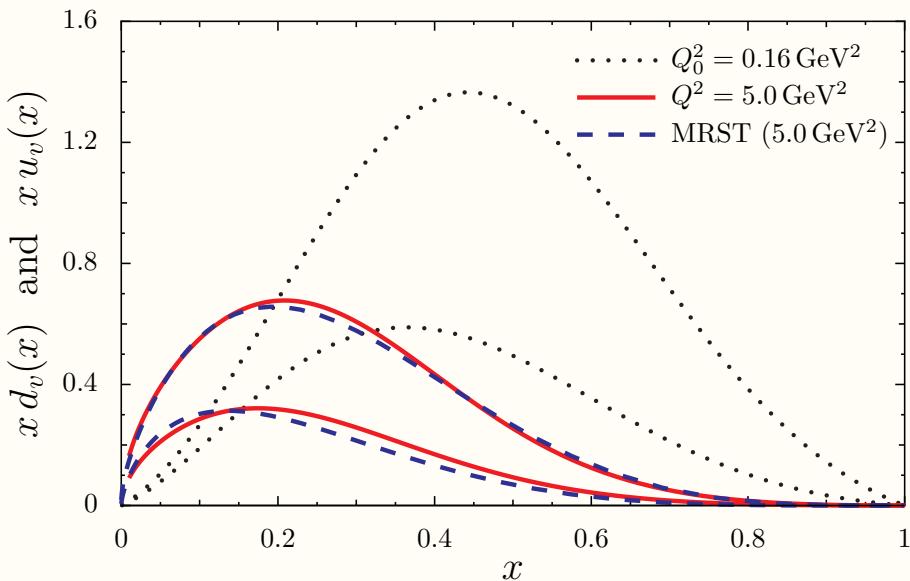
$$q(x) = p^+ \int \frac{d\xi^-}{2\pi} e^{i x p^+ \xi^-} \langle p, s | \bar{\psi}_q(0) \gamma^+ \psi_q(\xi^-) | p, s \rangle_c, \quad \Delta q(x) = \langle \gamma^+ \gamma_5 \rangle$$

- Associated with a Feynman diagram calculation



❖  $[q(x), \Delta q(x), \Delta_T q(x)] \rightarrow X = \delta \left( x - \frac{k^+}{p^+} \right) [\gamma^+, \gamma^+ \gamma_5, \gamma^+ \gamma^1 \gamma_5]$

# Results: proton quark distributions

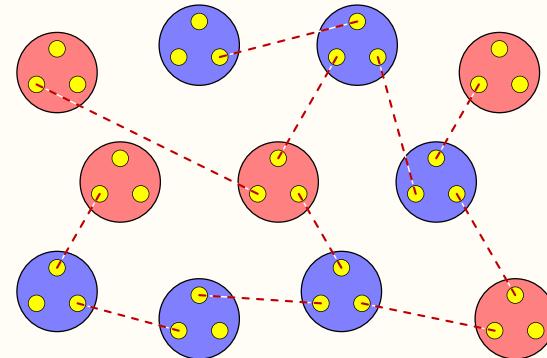
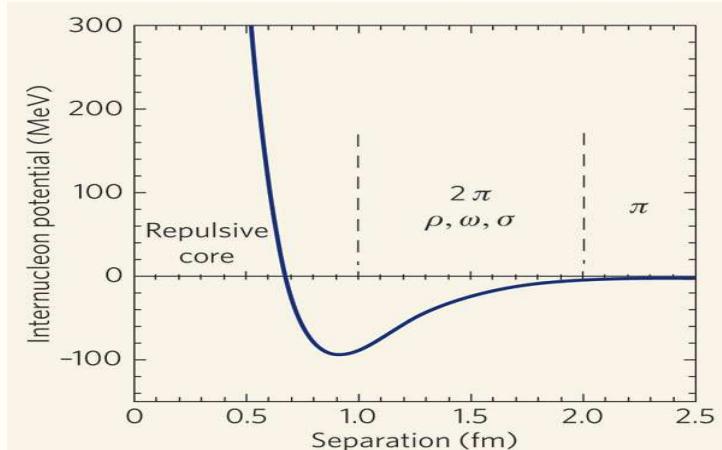


- Empirical distributions:
  - ◆ Martin, Roberts, Stirling and Thorne, Phys. Lett. B **531**, 216 (2002).
  - ◆ M. Hirai, S. Kumano and N. Saito, Phys. Rev. D **69**, 054021 (2004).
- NJL model gives good description of free nucleon quark distributions
- Approach is covariant, satisfies all sum rules & positivity constraints
- DGLAP equations [Dokshitzer (1977), Gribov-Lipatov (1972), Altarelli-Parisi (1977)]

$$\frac{\partial}{\partial \ln Q^2} q_v(x, Q^2) = \alpha_s(Q^2) P(z) \otimes q_v(y, Q^2)$$

# Asymmetric Nuclear Matter

- Fundamental physics: mean fields couple to the quarks in nucleons



- Finite density mean-field Lagrangian:  $\sigma$ ,  $\omega$ ,  $\rho$  fields

$$\mathcal{L} = \bar{\psi} (i \not{\partial} - M^* - \not{V}) \psi + \mathcal{L}'_I$$

- ◆  $\sigma$ : isoscalar-scalar – attractive
- $\omega$ : isoscalar-vector – repulsive
- $\rho$ : isovector-vector – attractive/repulsive

- Finite density quark propagator

$$S(k)^{-1} = \not{k} - M - i\varepsilon \quad \rightarrow \quad S_q(k)^{-1} = \not{k} - M^* - \not{V}_q - i\varepsilon$$

# Effective Potential

- Hadronization → Effective potential

$$\mathcal{E} = \mathcal{E}_V - \frac{\omega_0^2}{4G_\omega} - \frac{\rho_0^2}{4G_\rho} + \mathcal{E}_p + \mathcal{E}_n$$

- ◆  $\mathcal{E}_V$ : vacuum energy  
 $\mathcal{E}_{p(n)}$ : energy of nucleons moving in  $\sigma$ ,  $\omega$ ,  $\rho$  fields

- Effective potential provides

$$\omega_0 = 6G_\omega(\rho_p + \rho_n), \quad \rho_0 = 2G_\rho(\rho_p - \rho_n), \quad \frac{\partial \mathcal{E}}{\partial M^*} = 0$$

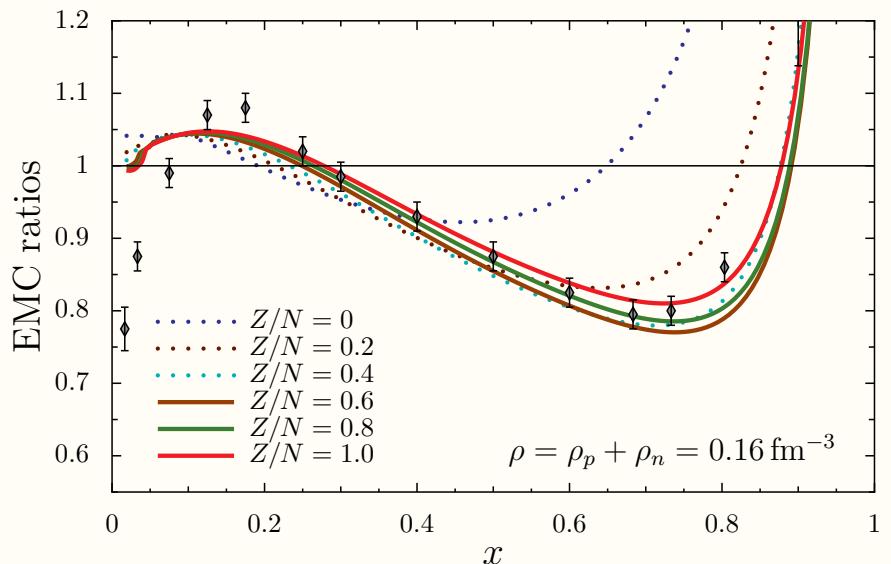
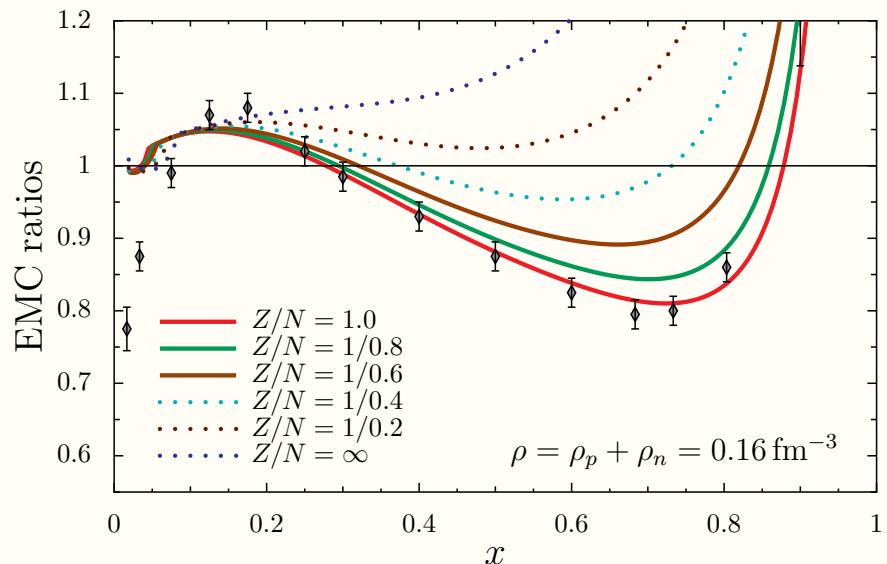
- ◆  $G_\omega \Leftrightarrow Z = N$  saturation &  $G_\rho \Leftrightarrow$  symmetry energy

- Quark vector fields:

$$V_{u(d)} = \omega_0 \pm \rho_0$$

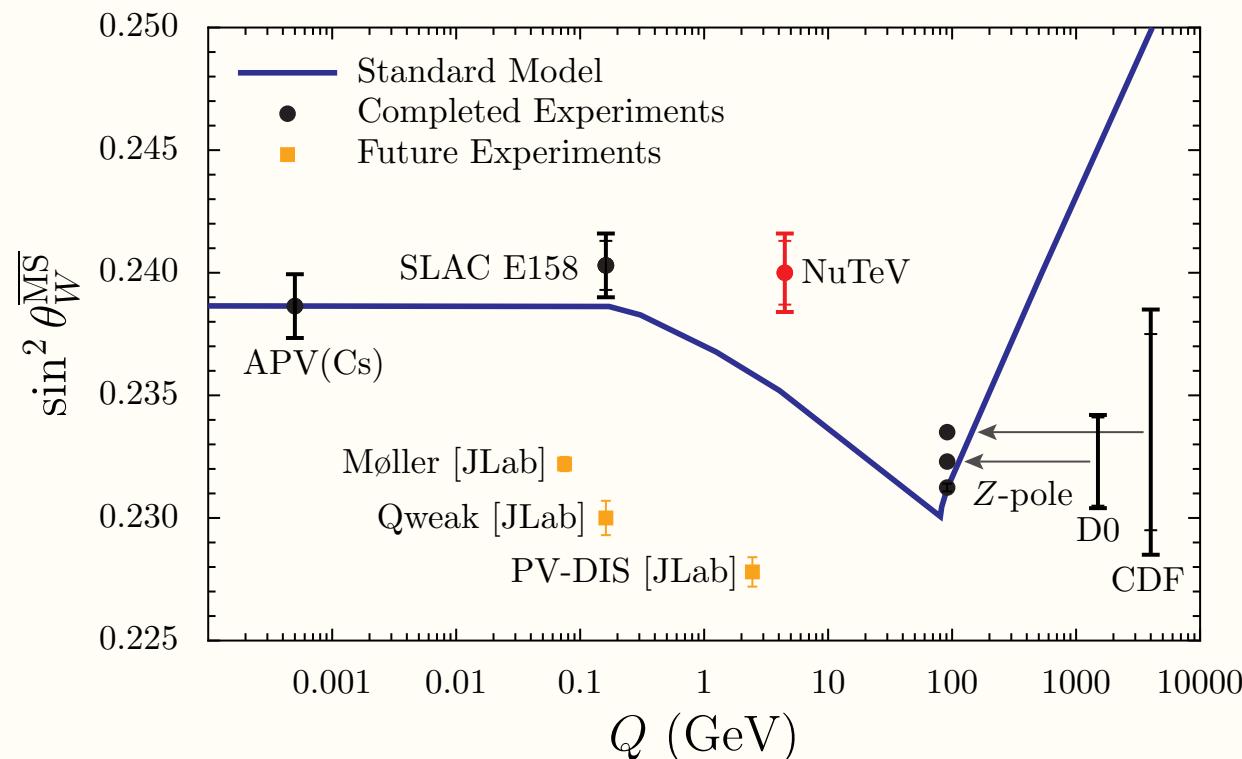
- Recall: quark propagator:  $S_q(k) = [\not{k} - M^* - \not{V}_q]^{-1}$

# Isovector EMC effect



- **EMC ratio:** 
$$R = \frac{F_{2A}}{F_{2A}^{\text{naive}}} = \frac{F_{2A}}{Z F_{2p} + N F_{2n}} \sim \frac{4 u_A(x) + d_A(x)}{4 u_0(x) + d_0(x)}$$
- Density is fixed only  $Z/N$  ratio is changing
  - ◆ non-trivial isospin dependence
- proton excess:  $u$ -quarks feel more repulsion than  $d$ -quarks
- neutron excess:  $d$ -quarks feel more repulsion than  $u$ -quarks
- Isovector interaction  $\implies$  isovector EMC Effect

# Weak mixing angle and the NuTeV anomaly



- NuTeV:  $\sin^2 \theta_W = 0.2277 \pm 0.0013(\text{stat}) \pm 0.0009(\text{syst})$ 
  - ◆ G. P. Zeller et al. Phys. Rev. Lett. **88**, 091802 (2002)
- World average  $\sin^2 \theta_W = 0.2227 \pm 0.0004$  :  $3\sigma \implies \text{"NuTeV anomaly"}$
- Huge amount of experimental & theoretical interest [over 400 citations]
- No universally accepted complete explanation

# Paschos-Wolfenstein ratio

- Paschos-Wolfenstein ratio motivated the NuTeV study:

$$R_{PW} = \frac{\sigma_{NC}^{\nu A} - \sigma_{NC}^{\bar{\nu} A}}{\sigma_{CC}^{\nu A} - \sigma_{CC}^{\bar{\nu} A}}, \quad NC \Rightarrow Z^0, \quad CC \Rightarrow W^\pm$$

- Expressing  $R_{PW}$  in terms of quark distributions:

$$R_{PW} = \frac{\left(\frac{1}{6} - \frac{4}{9} \sin^2 \theta_W\right) \langle x u_A^- \rangle + \left(\frac{1}{6} - \frac{2}{9} \sin^2 \theta_W\right) \langle x d_A^- + x s_A^- \rangle}{\langle x d_A^- + x s_A^- \rangle - \frac{1}{3} \langle x u_A^- \rangle}$$

- For an isoscalar target  $u_A \simeq d_A$  and if  $s_A \ll u_A + d_A$

$$R_{PW} = \frac{1}{2} - \sin^2 \theta_W + \Delta R_{PW}$$

- NuTeV measured  $R_{PW}$  on an Fe target ( $Z/N \simeq 26/30$ )
- Correct for neutron excess  $\Leftrightarrow$  isoscalarity corrections

# Isovector EMC correction to NuTeV

- General form of isoscalarity corrections

$$R_{PW} = \left( \frac{1}{2} - \sin^2 \theta_W \right) + \left( 1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x u_A^- - x d_A^- \rangle}{\langle x u_A^- + x d_A^- \rangle}$$

- NuTeV assumed nucleons in Fe are like free nucleons
  - Ignored some medium effects: Fermi motion &  $\rho^0$ -field
- Use our medium modified “Fe” quark distributions

$$\begin{aligned}\Delta R_{PW} &= \Delta R_{PW}^{\text{naive}} + \Delta R_{PW}^{\text{Fermi}} + \Delta R_{PW}^{\rho^0} \\ &= -(0.0107 + 0.0004 + 0.0028).\end{aligned}$$

- Recall NuTeV requires  $\Delta R_{PW} = -0.005$

$$\begin{aligned}R_{PW}^{\text{SM}} &\equiv 0.2773 \pm \dots \quad (= \frac{1}{2} - \sin^2 \theta_W) \\ R_{PW}^{\text{NuTeV}} &= 0.2723 \pm \dots\end{aligned}$$

- Isoscalarity  $\rho^0$  correction can explain up to 65% of anomaly

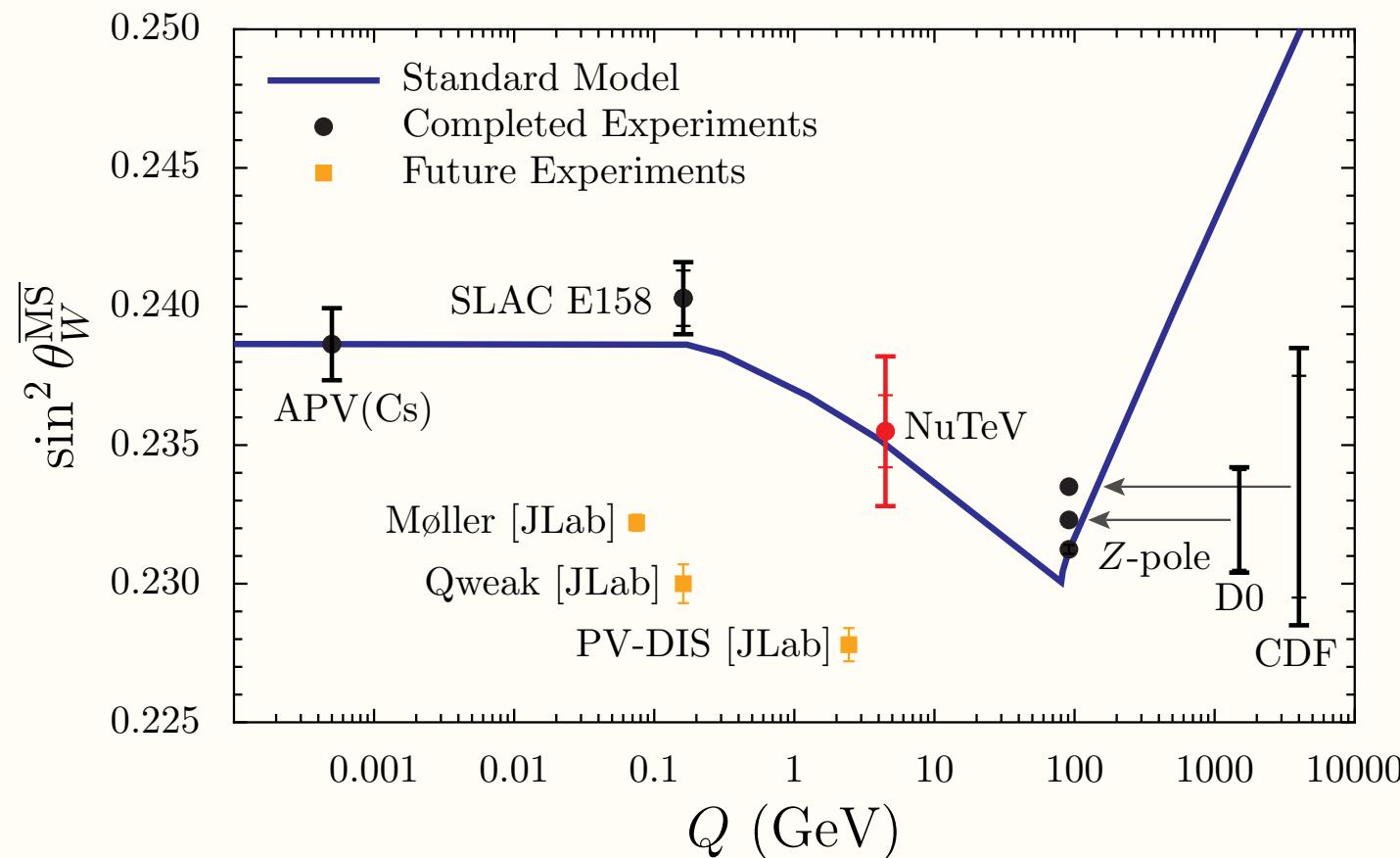
## NuTeV anomaly cont'd

- Also correction from  $m_u \neq m_d$  - Charge Symmetry Violation
  - ◆ CSV +  $\rho_0 \implies$  no NuTeV anomaly
  - ◆ No evidence for physics beyond the Standard Model
- Instead “NuTeV anomaly” is evidence for medium modification
  - ◆ Equally interesting
  - ◆ EMC effect has over 850 citations [J. J. Aubert *et al.*, Phys. Lett. B 123, 275 (1983).]
- Model dependence?
  - ◆ sign of correction is fixed by nature of vector fields

$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left( \frac{p^+}{p^+ - V^+} - \frac{V_q^+}{p^+ - V^+} \right), \quad N > Z \implies V_d > V_u$$

  - ◆  $\rho^0$ -field shifts momentum from  $u$ - to  $d$ -quarks
  - ◆ size of correction is constrained by Nucl. Matt. symmetry energy
- $\rho_0$  vector field reduces NuTeV anomaly – Model Independent!!

# Total NuTeV correction



- Includes NuTeV functionals
- Small increase in systematic error
- NuTeV anomaly interpreted as evidence for medium modification
- Equally profound as evidence for physics beyond Standard Model

# Consistent with other observables?

- We claim isovector EMC effect explains  $\sim 1.5\sigma$  of NuTeV result
  - ◆ is this mechanism observed elsewhere?
- Yes!! Parity violating DIS:  $\gamma Z^0$  interference

$$A_{PV} = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L} \propto \left[ a_2(x) + \frac{1 - (1 - y)^2}{1 + (1 - y)^2} a_3(x) \right]$$

$$a_2(x) = -2g_A^e \frac{F_2^{\gamma Z}}{F_2^\gamma} = \frac{6u^+ + 3d^+}{4u^+ + d^+} - 4\sin^2\theta_W$$

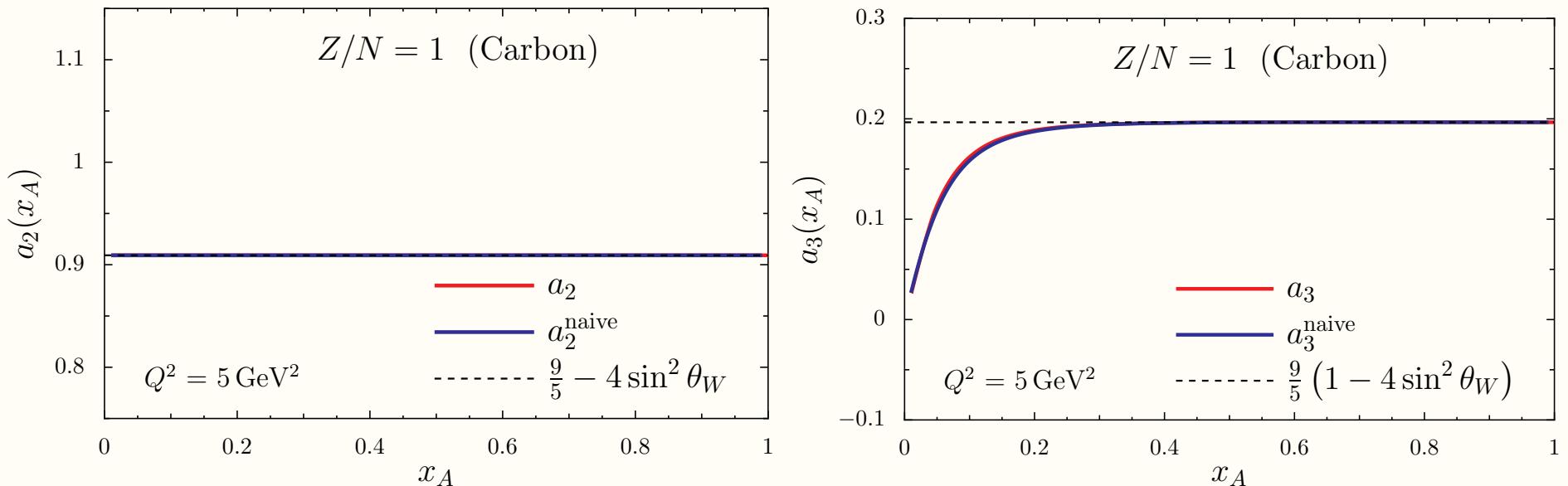
$$a_3(x) = -2g_V^e \frac{F_3^{\gamma Z}}{F_2^\gamma} = 3(1 - 4\sin^2\theta_W) \frac{2u^- + d^-}{4u^+ + d^+}$$

- Parton model expressions

$$F_2^{\gamma Z} = 2 \sum e_q g_V^q x (q + \bar{q}), \quad g_V^q = \pm \frac{1}{2} - 2e_q \sin^2\theta_W$$

$$F_3^{\gamma Z} = 2 \sum e_q g_A^q (q - \bar{q}), \quad g_A^q = \pm \frac{1}{2}$$

# Parity Violating DIS: Carbon



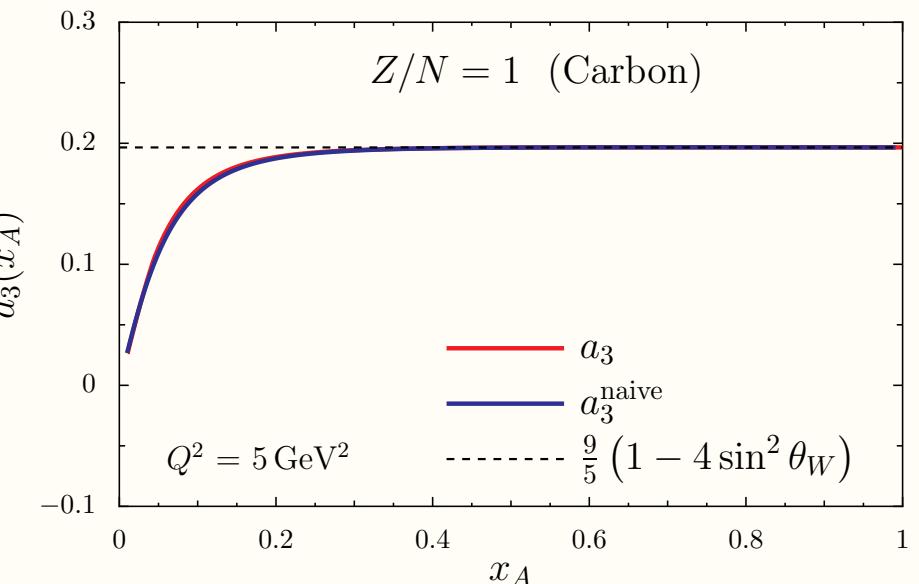
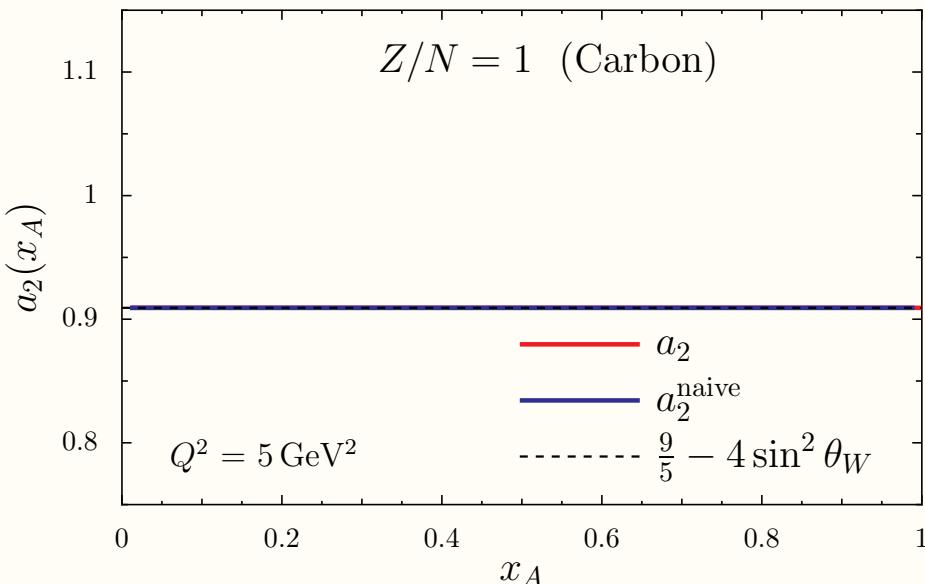
- Ignoring quark mass differences,  $s$ -quarks and EW corrections
  - For a  $N = Z$  target:

$$a_2(x) = \frac{6u_A^+ + 3d_A^+}{4u_A^+ + d_A^+} - 4 \sin^2 \theta_W \rightarrow \frac{9}{5} - 4 \sin^2 \theta_W$$

$$a_3(x) = 3(1 - 4 \sin^2 \theta_W) \frac{2u^-_A + d^-_A}{4u_A^+ + d_A^+} \rightarrow \frac{9}{5}(1 - 4 \sin^2 \theta_W) \frac{u^-_A + d^-_A}{u_A^+ + d_A^+}$$

- Measurement of  $a_2(x)$  at each  $x \implies$  a NuTeV experiment!

# Parity Violating DIS: Carbon



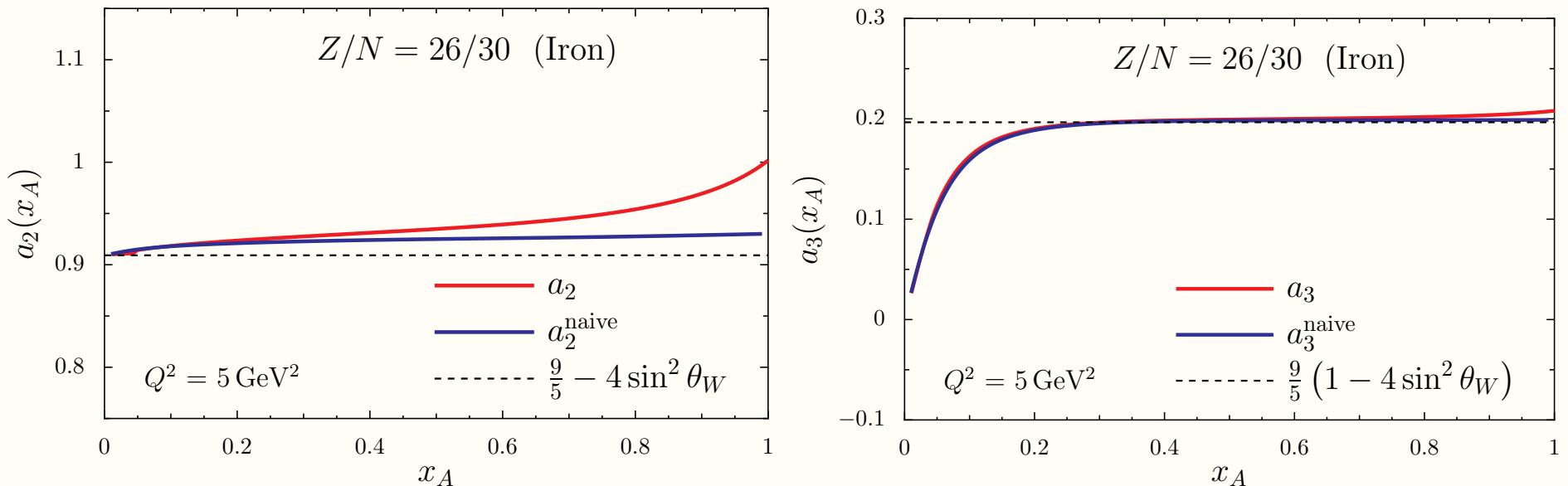
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$$a_2(x) = \frac{6u_A^+ + 3d_A^+}{4u_A^+ + d_A^+} - 4 \sin^2 \theta_W \rightarrow \frac{9}{5} - 4 \sin^2 \theta_W$$

$$a_3(x) \rightarrow \frac{9}{5} (1 - 4 \sin^2 \theta_W) \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} = \frac{9}{5} (1 - 4 \sin^2 \theta_W) \left[ 1 + 2 \frac{\bar{u}_A + \bar{d}_A}{u_A^- + d_A^-} \right]^{-1}$$

- Measurement of  $a_2(x)$  at each  $x \implies$  a NuTeV experiment!

# Parity Violating DIS: Iron



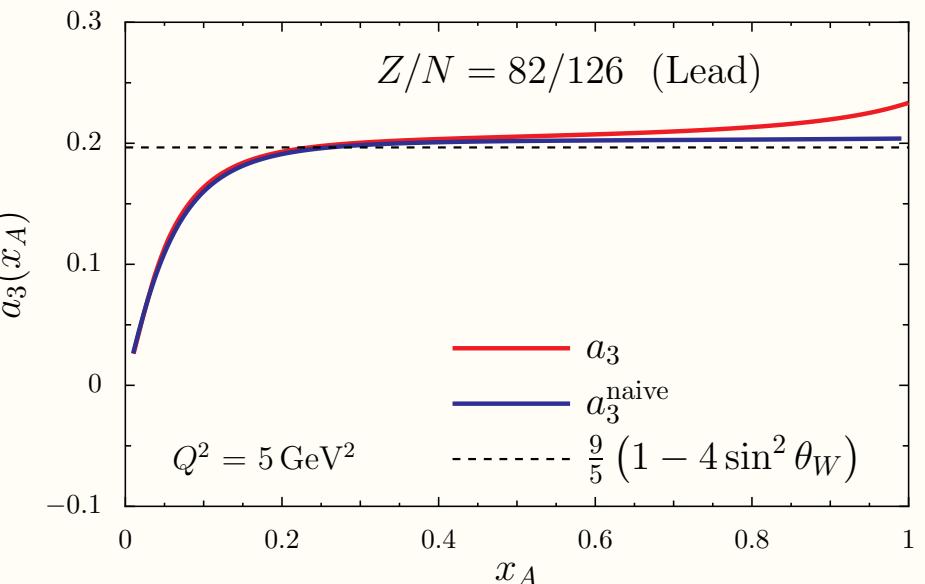
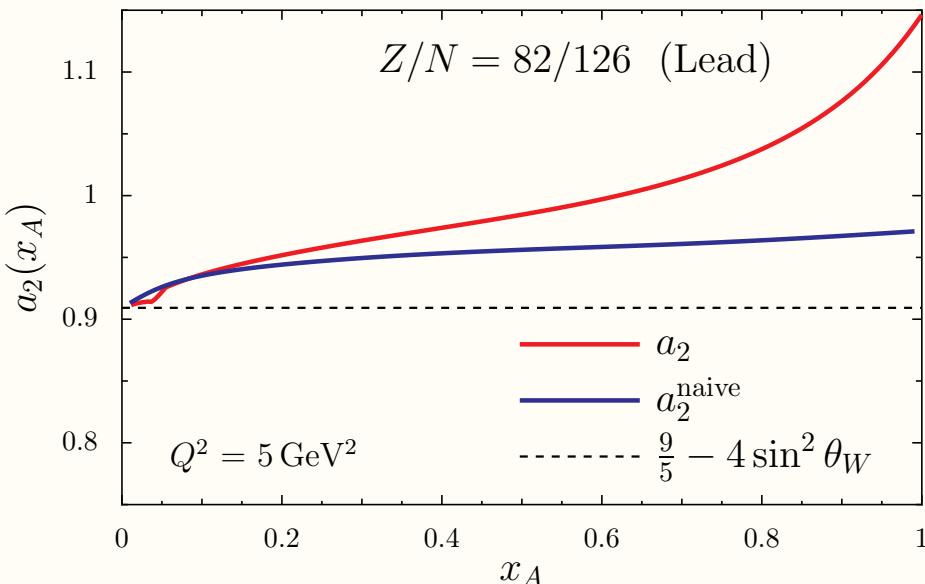
- For a  $N \simeq Z$  target:

$$a_2(x) = \frac{9}{5} - 4 \sin^2 \theta_W - \frac{12}{25} \frac{u_A^+(x) - d_A^+(x)}{u_A^+(x) + d_A^+(x)}$$

$$a_3(x) = \frac{9}{5} (1 - 4 \sin^2 \theta_W) \left\{ \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} - \frac{1}{3} \left[ \frac{12}{5} \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} \frac{u_A^+ - d_A^+}{u_A^+ + d_A^+} - \frac{u_A^- - d_A^-}{u_A^+ + d_A^+} \right] \right\}$$

- “Naive” result has no medium corrections
- Sizeable medium effects in  $a_2(x)$

# Parity Violating DIS: Lead



- For a  $N \simeq Z$  target:

$$a_2(x) = \frac{9}{5} - 4 \sin^2 \theta_W - \frac{12}{25} \frac{u_A^+(x) - d_A^+(x)}{u_A^+(x) + d_A^+(x)}$$

$$a_3(x) = \frac{9}{5} (1 - 4 \sin^2 \theta_W) \left\{ \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} - \frac{1}{3} \left[ \frac{12}{5} \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} \frac{u_A^+ - d_A^+}{u_A^+ + d_A^+} - \frac{u_A^- - d_A^-}{u_A^+ + d_A^+} \right] \right\}$$

- After naive isoscalarity corrections medium effects still very large
- Large  $x$  dependence of  $a_2(x) \rightarrow$  evidence for medium modification

# Finite nuclei EMC effects

- EMC ratio

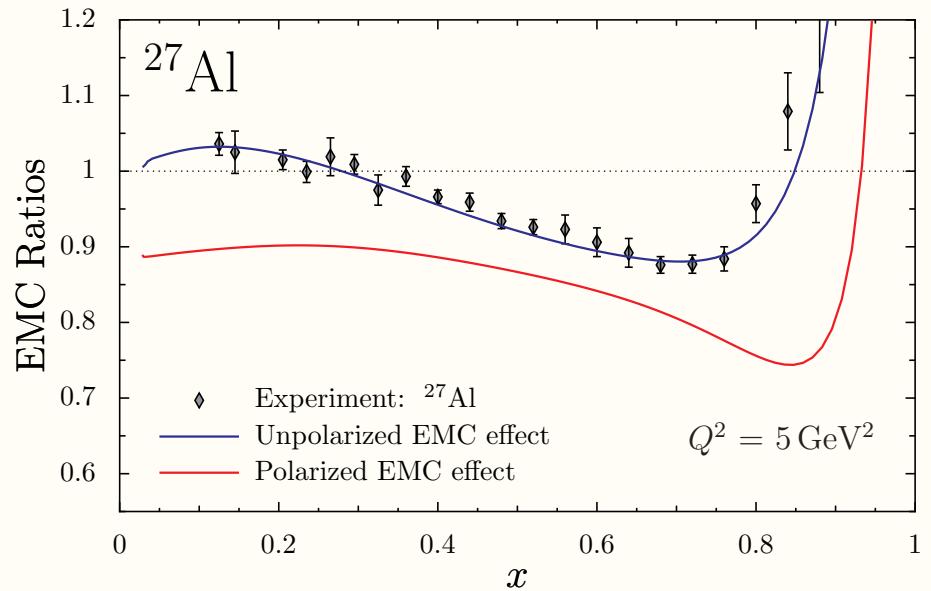
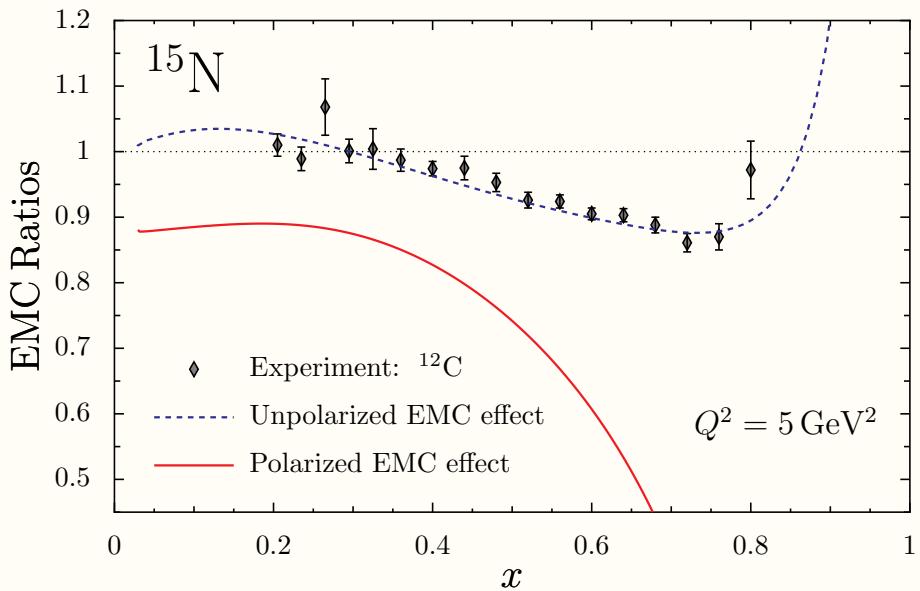
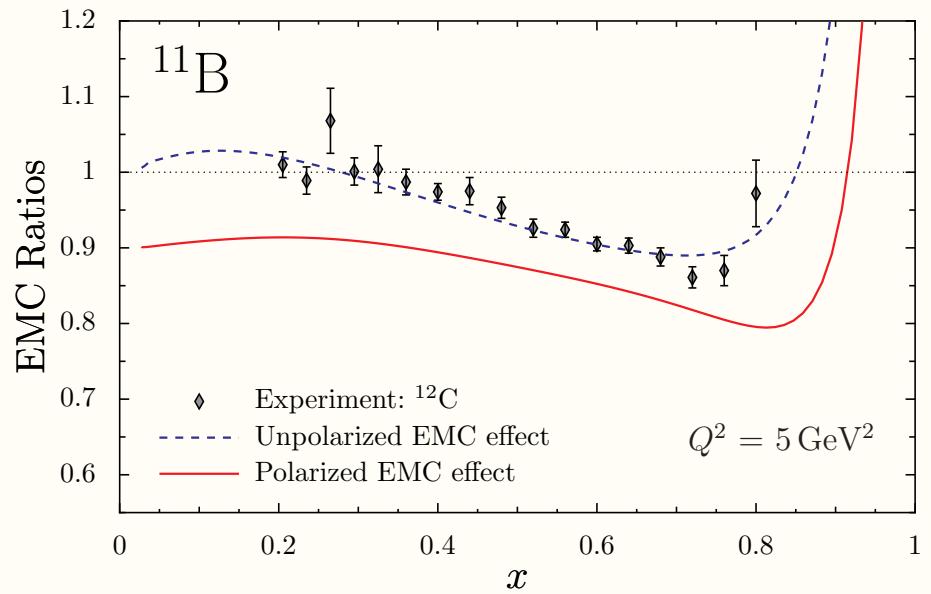
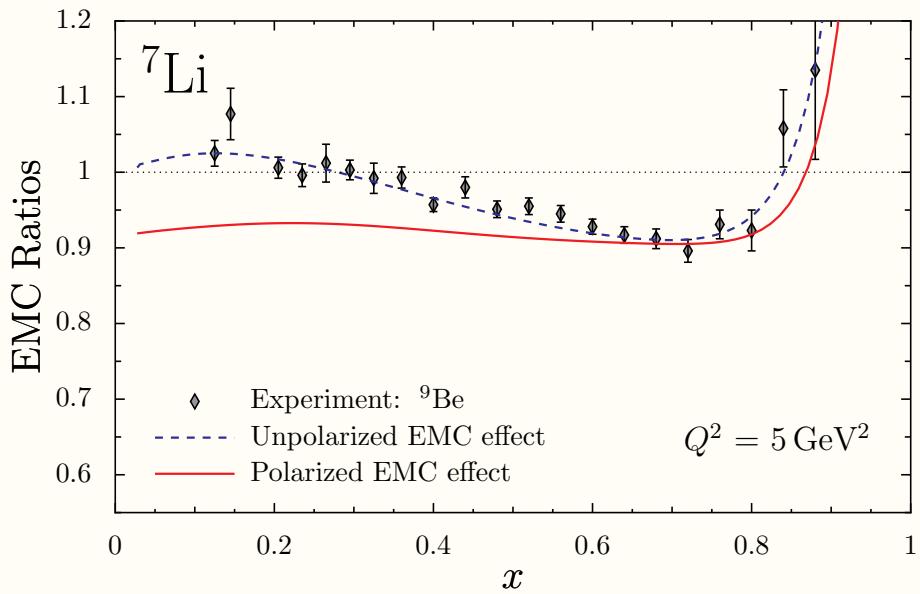
$$R = \frac{F_{2A}}{F_{2A}^{\text{naive}}} = \frac{F_{2A}}{Z F_{2p} + N F_{2n}}$$

- Polarized EMC ratio

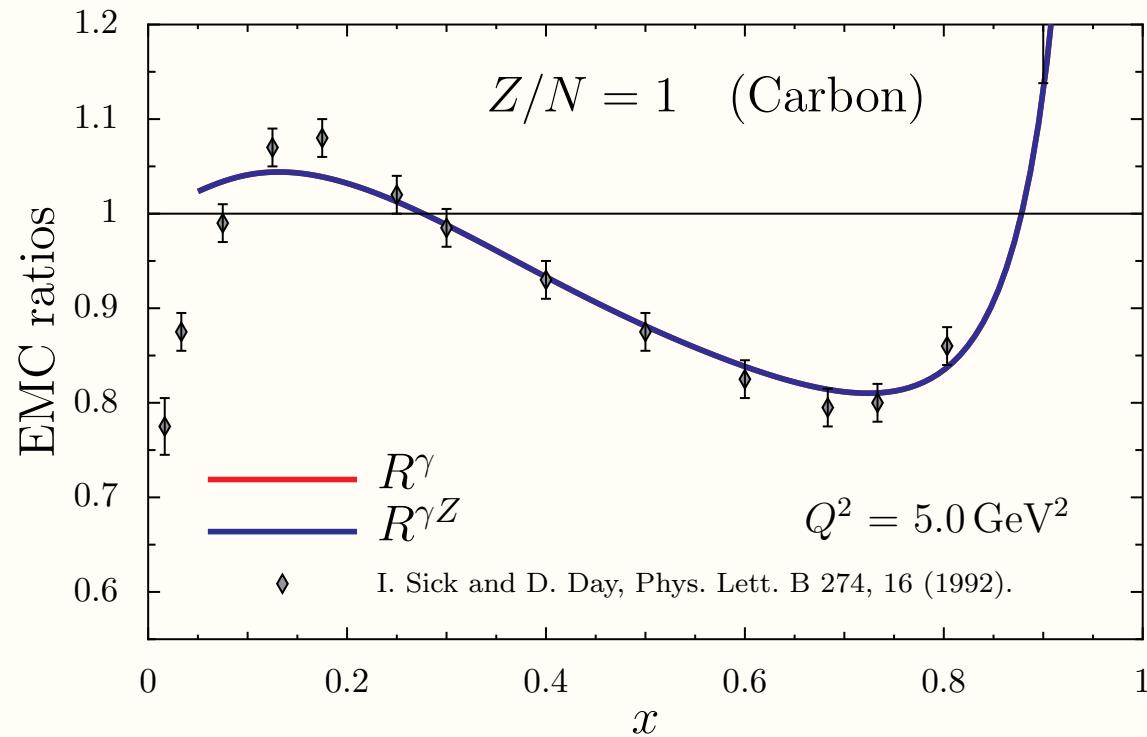
$$R_s^H = \frac{g_{1A}^H}{g_{1A}^{H,\text{naive}}} = \frac{g_{1A}^H}{P_p^H g_{1p} + P_n^H g_{1n}}$$

- Spin-dependent cross-section is suppressed by  $1/A$ 
  - ◆ Must choose nuclei with  $A \lesssim 27$
  - ◆ protons should carry most of the spin e.g.  $\Rightarrow {}^7\text{Li}, {}^{11}\text{B}, \dots$
- Ideal nucleus is probably  ${}^7\text{Li}$ 
  - ◆ From Quantum Monte–Carlo:  $P_p^J = 0.86$  &  $P_n^J = 0.04$
- Ratios equal 1 in non-relativistic and no-medium modification limit

# EMC ratio $^7\text{Li}$ , $^{11}\text{B}$ , $^{15}\text{N}$ and $^{27}\text{Al}$



# $F_2^\gamma$ and $F_2^{\gamma Z}$ EMC ratios – “Carbon”

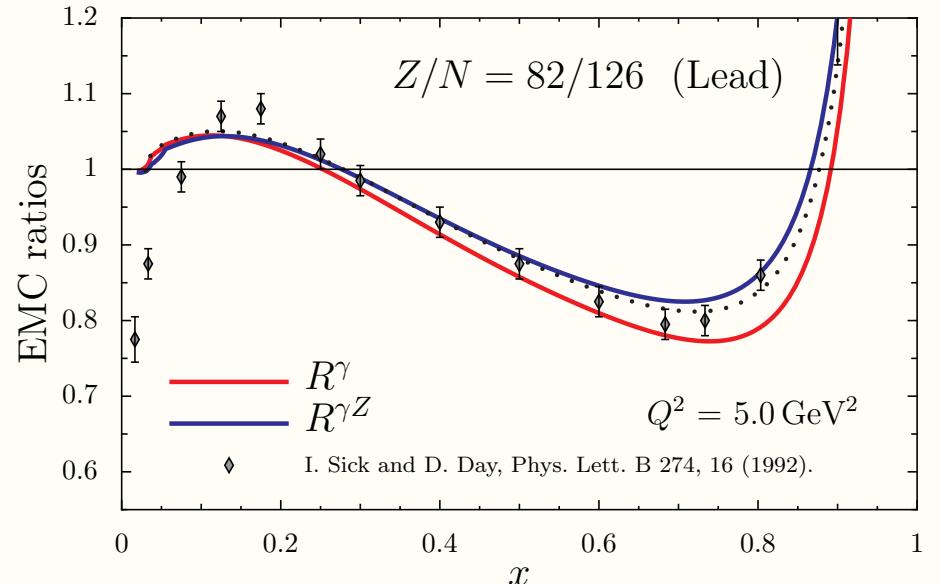
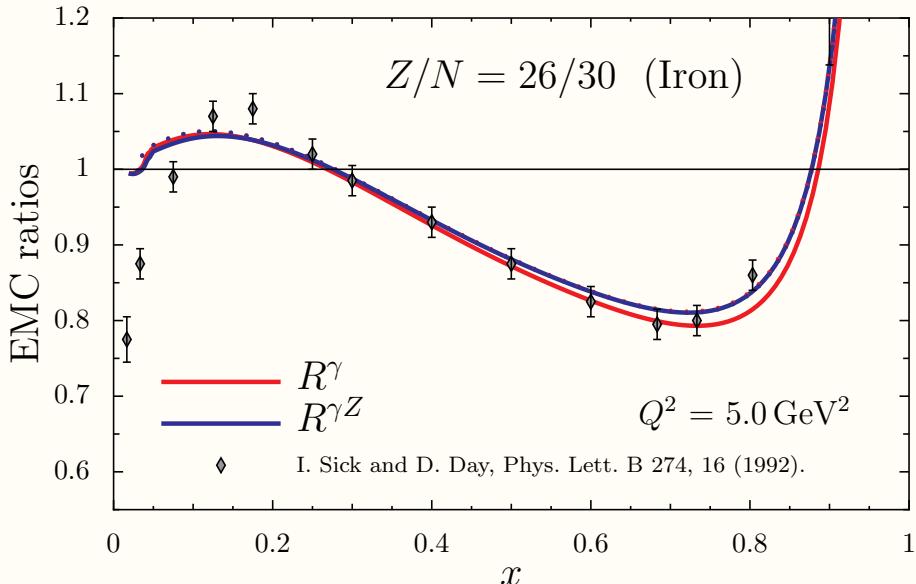


- Recall EMC ratio:

$$R^i = \frac{F_{2A}^i}{F_{2A}^{i,\text{naive}}} = \frac{F_{2A}^i}{Z F_{2p}^i + N F_{2n}^i} \quad i \in \gamma, \gamma Z, \dots$$

$$R^\gamma \sim \frac{4 u_A(x) + d_A(x)}{4 u_0(x) + d_0(x)}, \quad R^{\gamma Z} \sim \frac{1.16 u_A(x) + d_A(x)}{1.16 u_0(x) + d_0(x)}$$

# $F_2^\gamma$ and $F_2^{\gamma Z}$ EMC ratios – “Iron” & “Lead”

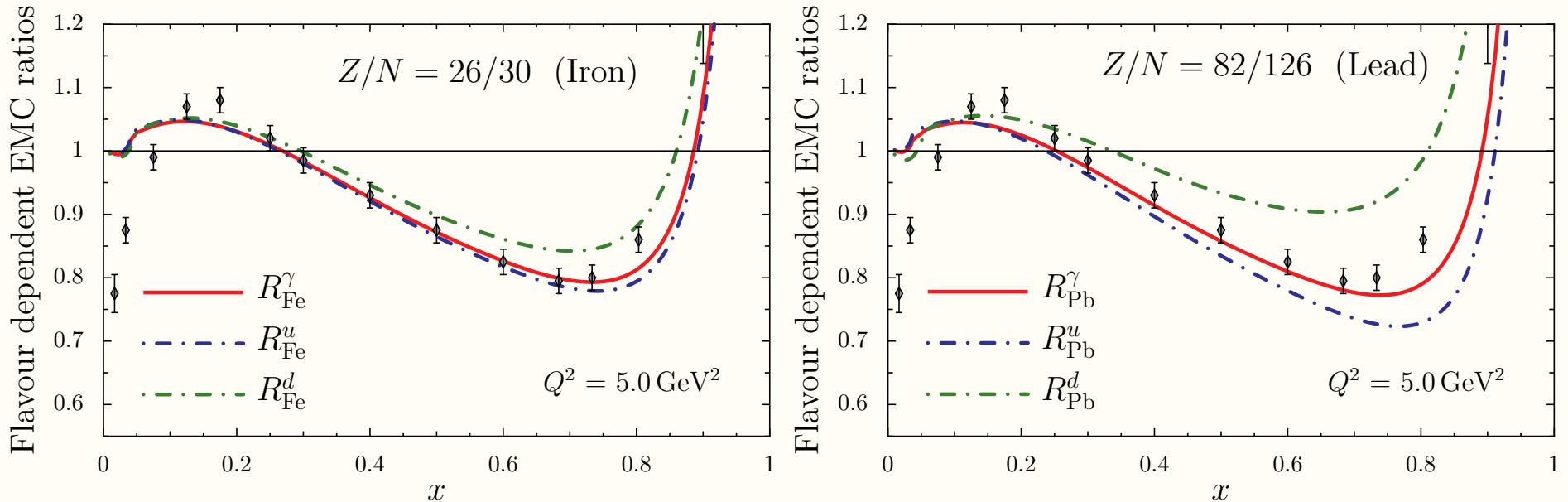


- $R^\gamma \sim \frac{4u_A(x)+d_A(x)}{4u_0(x)+d_0(x)}$  &  $R^{\gamma Z} \sim \frac{1.16u_A(x)+d_A(x)}{1.16u_0(x)+d_0(x)}$
- $u_A$  dominates  $R^\gamma$  where  $R^{\gamma Z}$  almost isoscalar ratio
- $N > Z$ :  $d$ -quarks feel more repulsion than  $u$ -quarks:  $V_d > V_u$

$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left( \frac{p^+}{p^+ - V^+} x - \frac{V_q^+}{p^+ - V^+} \right)$$

- $\rho_0$ -field  $\implies R^{\gamma Z} > R^\gamma$  – Model Independent

# Flavour Dependence of EMC effect

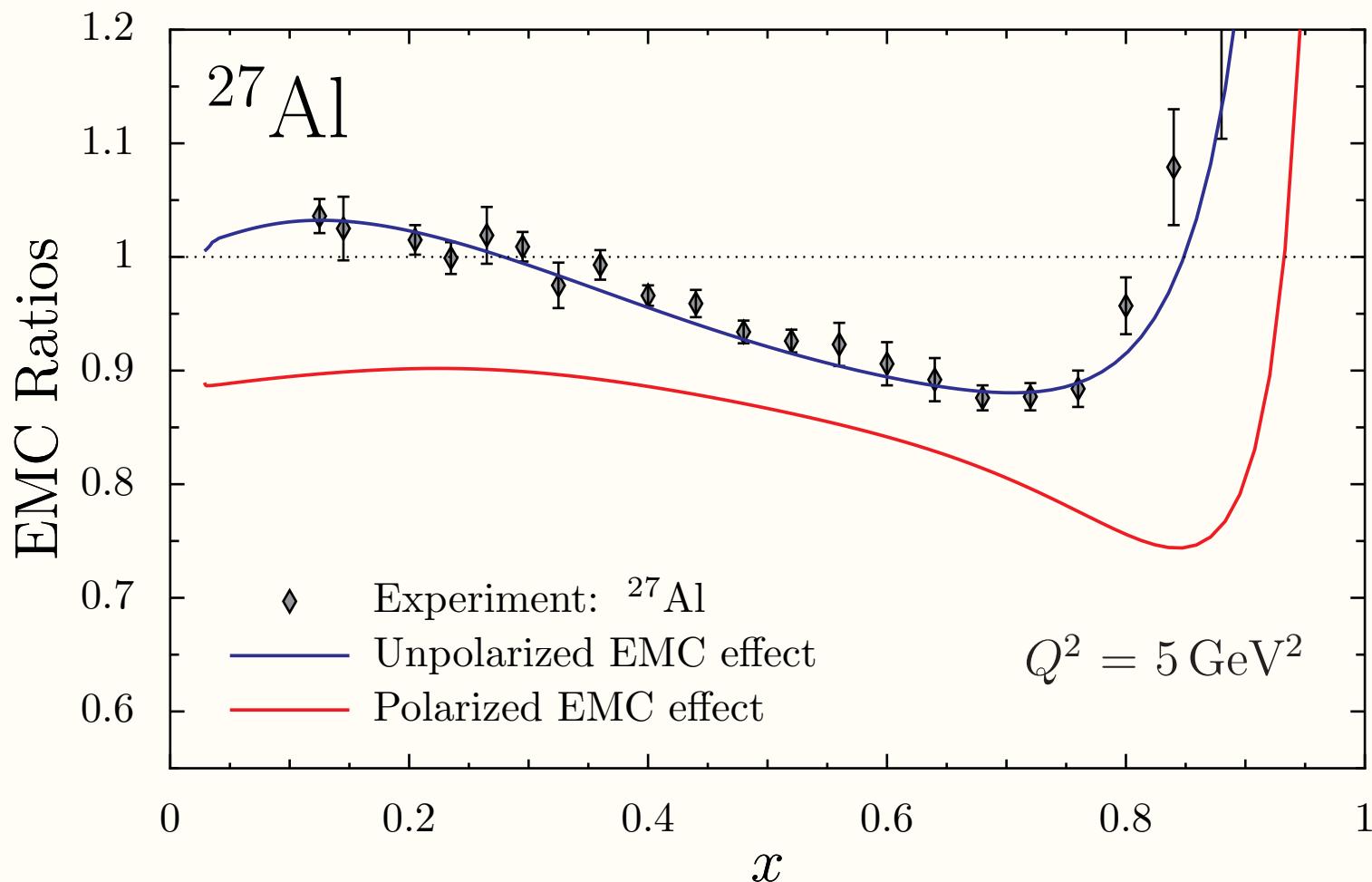


- Flavour dependence determined by measuring  $F_{2A}^{\gamma}$  and  $F_{2A}^{\gamma Z}$
- Defined above by

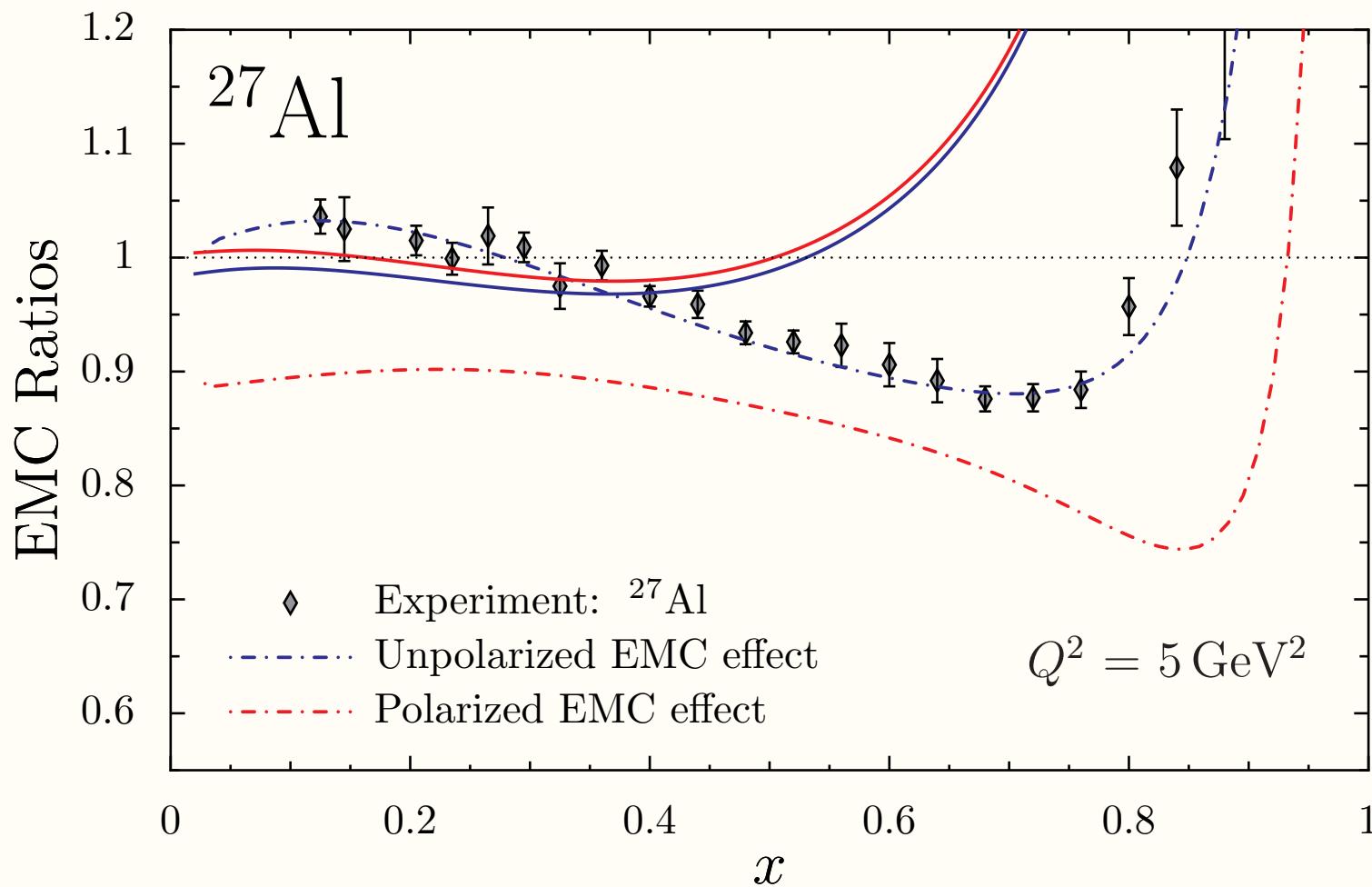
$$R_A^q = \frac{F_{2A}^q}{F_{2A}^{q, \text{naive}}} \simeq \frac{q_A}{q_0}$$

- If observed  $\Rightarrow$  very strong evidence for medium modification

# *Is there medium modification*



# *Is there medium modification*



- Medium modification of nucleon has been switched off
- Relativistic effects remain
- Large splitting would be strong evidence for medium modification

# Nuclear Spin Sum

Proton spin states	$\Delta u$	$\Delta d$	$\Sigma$	$g_A$
$p$	0.97	-0.30	0.67	1.267
${}^7\text{Li}$	0.91	-0.29	0.62	1.19
${}^{11}\text{B}$	0.88	-0.28	0.60	1.16
${}^{15}\text{N}$	0.87	-0.28	0.59	1.15
${}^{27}\text{Al}$	0.87	-0.28	0.59	1.15
Nuclear Matter	0.79	-0.26	0.53	1.05

- Angular momentum of nucleon:  $J = \frac{1}{2} = \frac{1}{2} \Delta \Sigma + L_q + J_g$ 
  - ◆ in medium  $M^* < M$  and therefore quarks are more relativistic
  - ◆ lower components of quark wavefunctions are enhanced
  - ◆ quark lower components usually have larger angular momentum
  - ◆  $\Delta q(x)$  very sensitive to lower components
- Conclusion: quark spin → orbital angular momentum in-medium

# Conclusion

- Effective quark theories can be used to incorporate quarks into a traditional description of nuclei
  - ◆ complementary approach to traditional nuclear physics
- Major outstanding discrepancy with Standard Model predictions for  $Z^0$  is NuTeV anomaly
  - ◆ may be resolved by CSV and isovector EMC effect corrections
- EMC effect and NuTeV anomaly are interpreted as evidence for medium modification of the bound nucleon wavefunction
- This result can be tested using PV DIS measurements
  - ◆ predict large medium modification in PV DIS
  - ◆ predict flavour dependence of EMC effect can be large
- Tried to demonstrate that PV DIS is a very powerful tool with which to study the parton structure of nuclei – at JLab or an EIC

# Model Parameters

- Free Parameters:  
 $\Lambda_{IR}$ ,  $\Lambda_{UV}$ ,  $M_0$ ,  $G_\pi$ ,  $G_s$ ,  $G_a$ ,  $G_\omega$  and  $G_\rho$
- Constraints:
  - ◆  $f_\pi = 93 \text{ MeV}$ ,  $m_\pi = 140 \text{ MeV}$  &  $M_N = 940 \text{ MeV}$
  - ◆  $\int_0^1 dx (\Delta u_v(x) - \Delta d_v(x)) = g_A = 1.267$
  - ◆  $(\rho, E_B/A) = (0.16 \text{ fm}^{-3}, -15.7 \text{ MeV})$
  - ◆  $a_4 = 32 \text{ MeV}$
  - ◆  $\Lambda_{IR} = 240 \text{ MeV}$
- We obtain [MeV]:
  - ◆  $\Lambda_{UV} = 644$
  - ◆  $M_0 = 400$ ,  $M_s = 690$ ,  $M_a = 990$ , ...
- Can now study a very large array of observables:
  - ◆ e.g. meson and baryon: quark distributions, form factors, GPDs, finite temp. and density, neutron stars

# Regularization

- Proper-time regularization

$$\frac{1}{X^n} = \frac{1}{(n-1)!} \int_0^\infty d\tau \tau^{n-1} e^{-\tau X}$$
$$\longrightarrow \frac{1}{(n-1)!} \int_{1/(\Lambda_{UV})^2}^{1/(\Lambda_{IR})^2} d\tau \tau^{n-1} e^{-\tau X}$$

- $\Lambda_{IR}$  eliminates unphysical thresholds for the nucleon to decay into quarks: → simulates confinement

◆ D. Ebert, T. Feldmann and H. Reinhardt, Phys. Lett. B **388**, 154 (1996).

- E.g.: Quark wave function renormalization

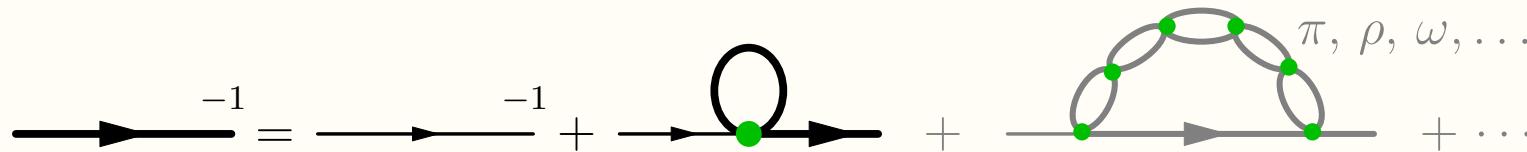
◆  $Z(k^2) = e^{-\Lambda_{UV}(k^2 - M^2)} - e^{-\Lambda_{IR}(k^2 - M^2)}$

→  $Z(k^2 = M^2) = 0 \implies \text{no free quarks}$

- Needed for: nuclear matter saturation,  $\Delta$  baryon, etc

◆ W. Bentz, A.W. Thomas, Nucl. Phys. A **696**, 138 (2001)

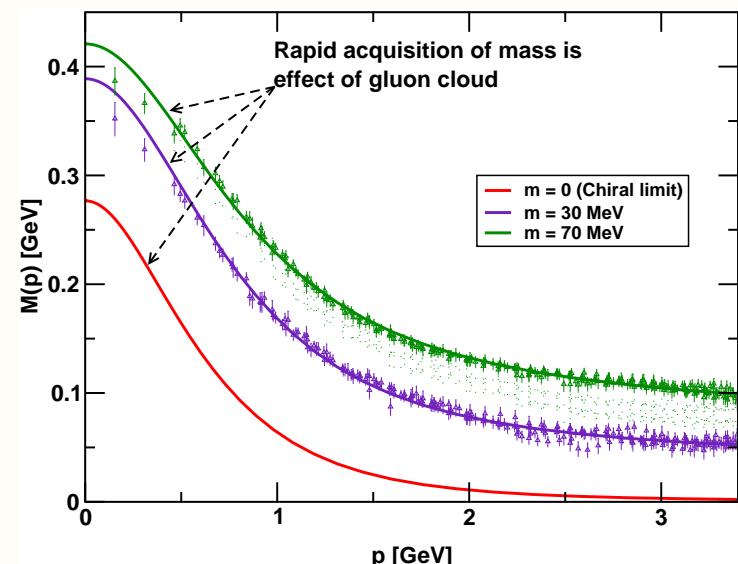
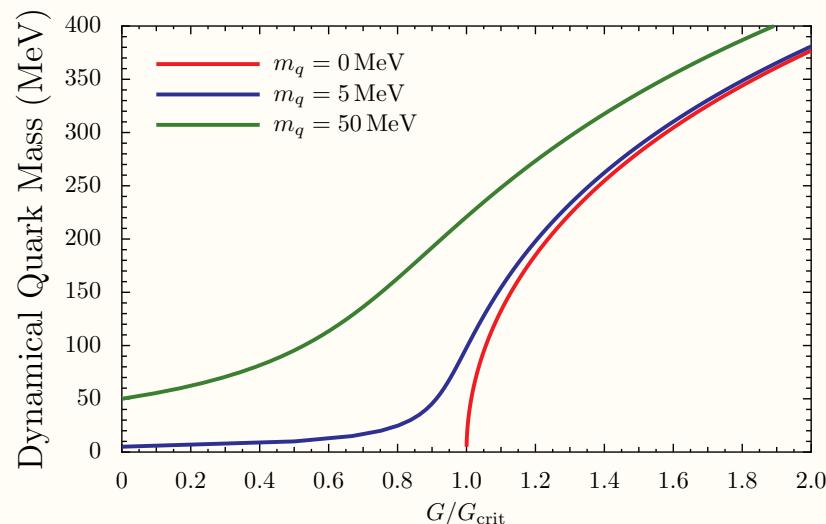
# Gap Equation & Mass Generation



- Quark Propagator:

$$\frac{1}{\not{p} - m + i\varepsilon} \rightarrow \frac{1}{\not{p} - M + i\varepsilon}$$

- Mass is generated via interaction with vacuum



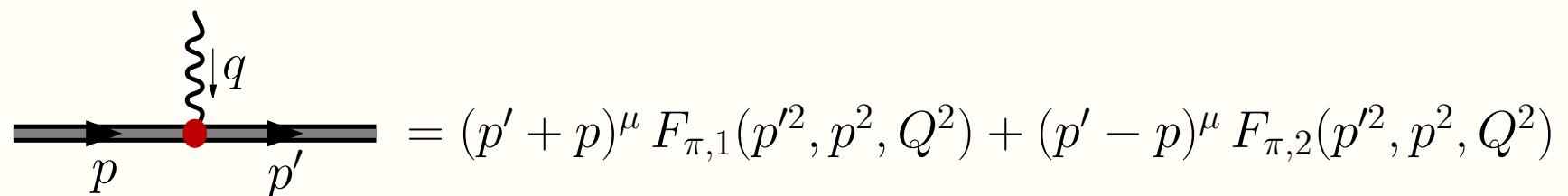
- Dynamically generated quark masses  $\iff \langle \bar{\psi} \psi \rangle \neq 0 \iff D\chi SB$
- Proper-time regularization:  $\Lambda_{IR}$  and  $\Lambda_{UV}$
- $\rightarrow$  No free quarks  $\implies$  Confinement  $[Z(k^2 = M^2) = 0]$

# Off-Shell Effects

- For an off-shell nucleon, photon–nucleon vertex given by

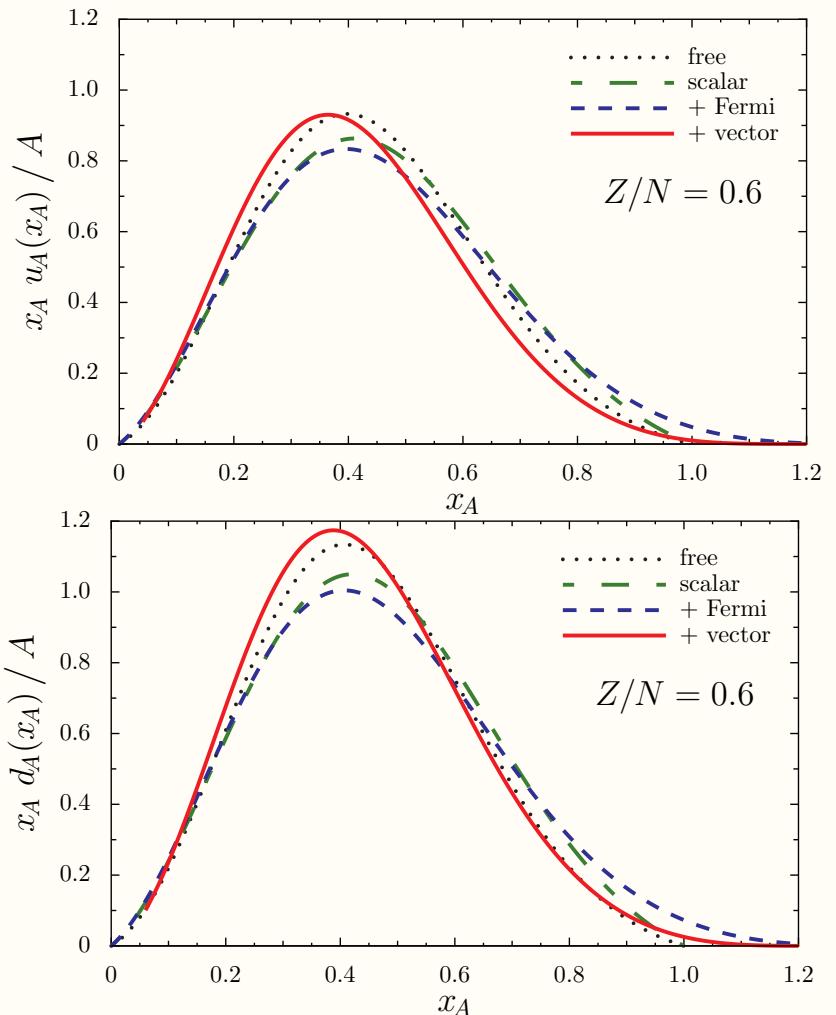
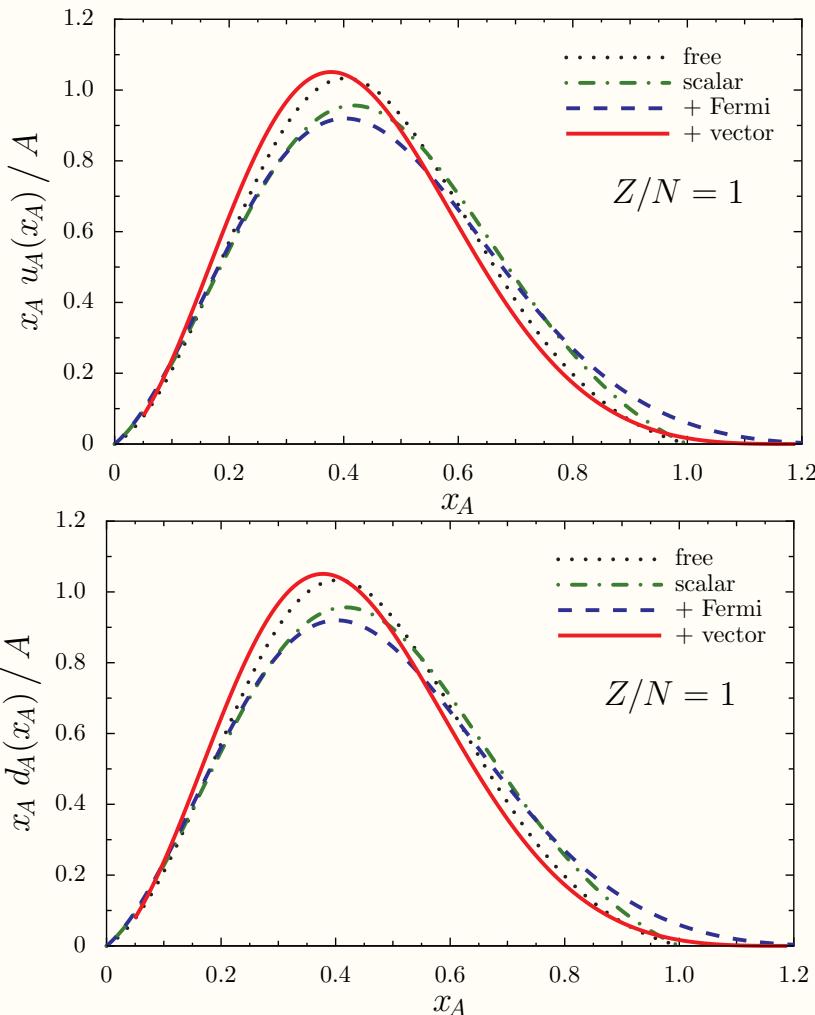
$$\Gamma_N^\mu(p', p) = \sum_{\alpha, \beta=+, -} \Lambda^\alpha(p') \left[ \gamma^\mu f_1^{\alpha\beta} + \frac{i\sigma^{\mu\nu} q_\nu}{2M} f_2^{\alpha\beta} + q^\mu f_3^{\alpha\beta} \right] \Lambda^\alpha(p)$$

- In-medium nucleon is off-shell, extremely difficult to quantify effects
  - However must understand to fully describe in-medium nucleon
- Simpler system: off-shell pion form factors
  - relax on-shell constraint  $p'^2 = p^2 = m_\pi^2$
  - Very difficult to calculate in many approaches, e.g. Lattice QCD



- For  $p'^2 = p^2 = m_\pi^2$  we have  $F_{\pi,1} \rightarrow F_\pi$  and  $F_{\pi,2} = 0$

# Results: Nuclear Matter



- $\rho_p + \rho_n = \text{fixed}$  – Differences arise from:
  - ◆ **naive:** different number protons and neutrons
  - ◆ **medium:**  $p$  &  $n$  Fermi motion and  $V_{u(d)}$  differ →  $u_p(x) \neq d_n(x), \dots$