

PV DIS Beyond Leading Twist

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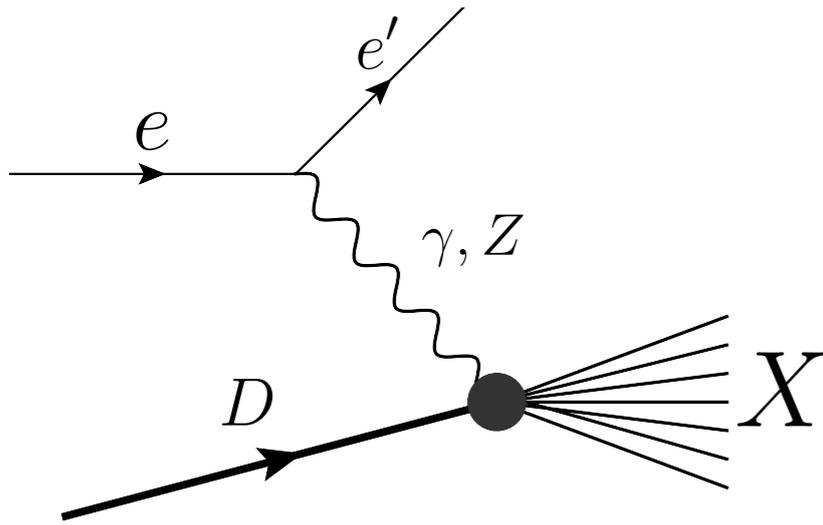
In Collaboration with M.J.Ramsey-Musolf and G.F. Sacco
arXiv:1004.3307

EIC, 2010, College of William and Mary, Williamsburg, VA

Outline

- Introductory Remarks
- PV DIS and Higher Twist
- Bjorken-Wolfenstein Argument
- Implications for interpreting experimental results
- Conclusions

Electron-Deuteron Asymmetry

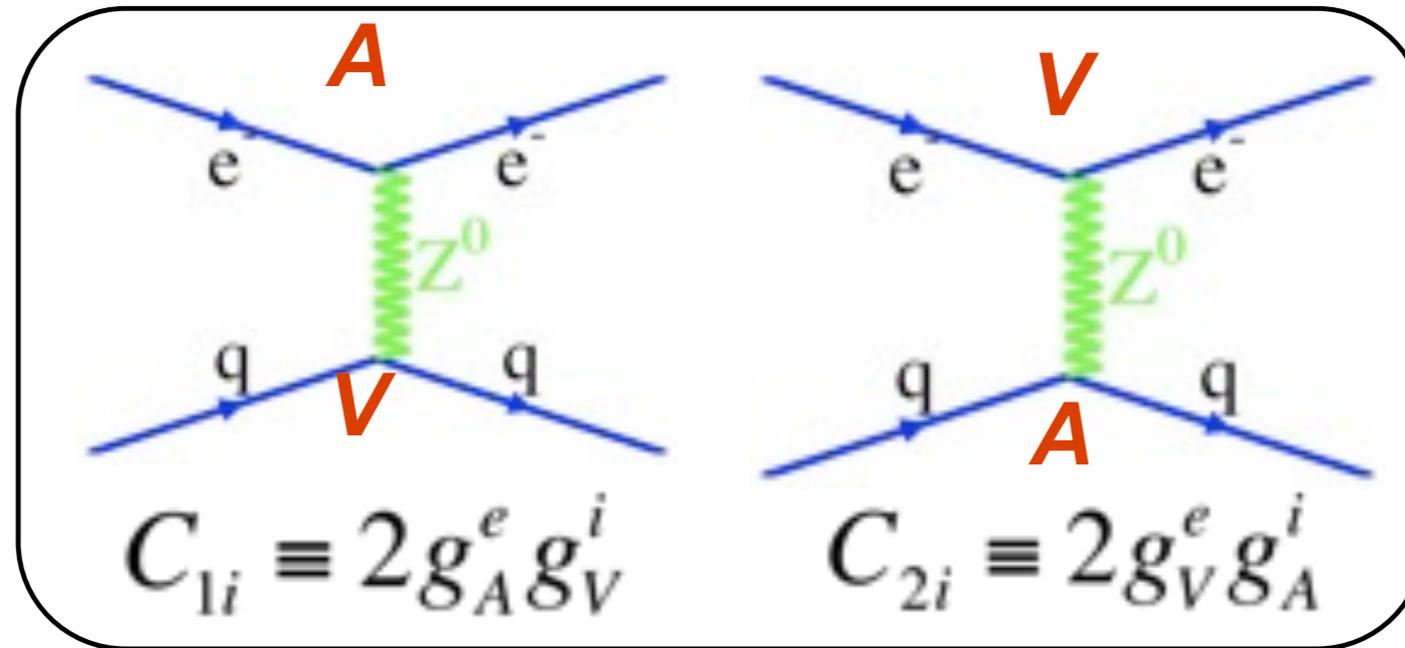


- Parity Violating asymmetry

$$A_{RL} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L}$$

- Probe of the parity-violating Weak Neutral Current (WNC) in the Standard Model (SM).
- Led to a spectacular confirmation of WNC theory of the SM in 1978 (SLAC).
- Gave one of the first precise measurements of the weak mixing angle to within 10%.

Electron-Deuteron Asymmetry



- Probe of parity-violating interactions in the Standard Model.

$$\mathcal{L} = \frac{G_F}{\sqrt{2}} \left[\bar{e} \gamma^\mu \gamma_5 e (C_{1u} \bar{u} \gamma_\mu u + C_{1d} \bar{d} \gamma_\mu d) + \bar{e} \gamma^\mu e (C_{2u} \bar{u} \gamma_\mu \gamma_5 u + C_{2d} \bar{d} \gamma_\mu \gamma_5 d) \right]$$

- Led to one of the first measurements of the weak mixing angle

$$C_{1u}^{\text{tree}} = -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W, \quad C_{1d}^{\text{tree}} = \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W,$$

$$C_{2u}^{\text{tree}} = -\frac{1}{2} + 2 \sin^2 \theta_W, \quad C_{2d}^{\text{tree}} = \frac{1}{2} - 2 \sin^2 \theta_W .$$

Electron-Deuteron Asymmetry

- All hadronic effects cancel in the asymmetry to first approximation; Cahn-Gilman (CG) formula:

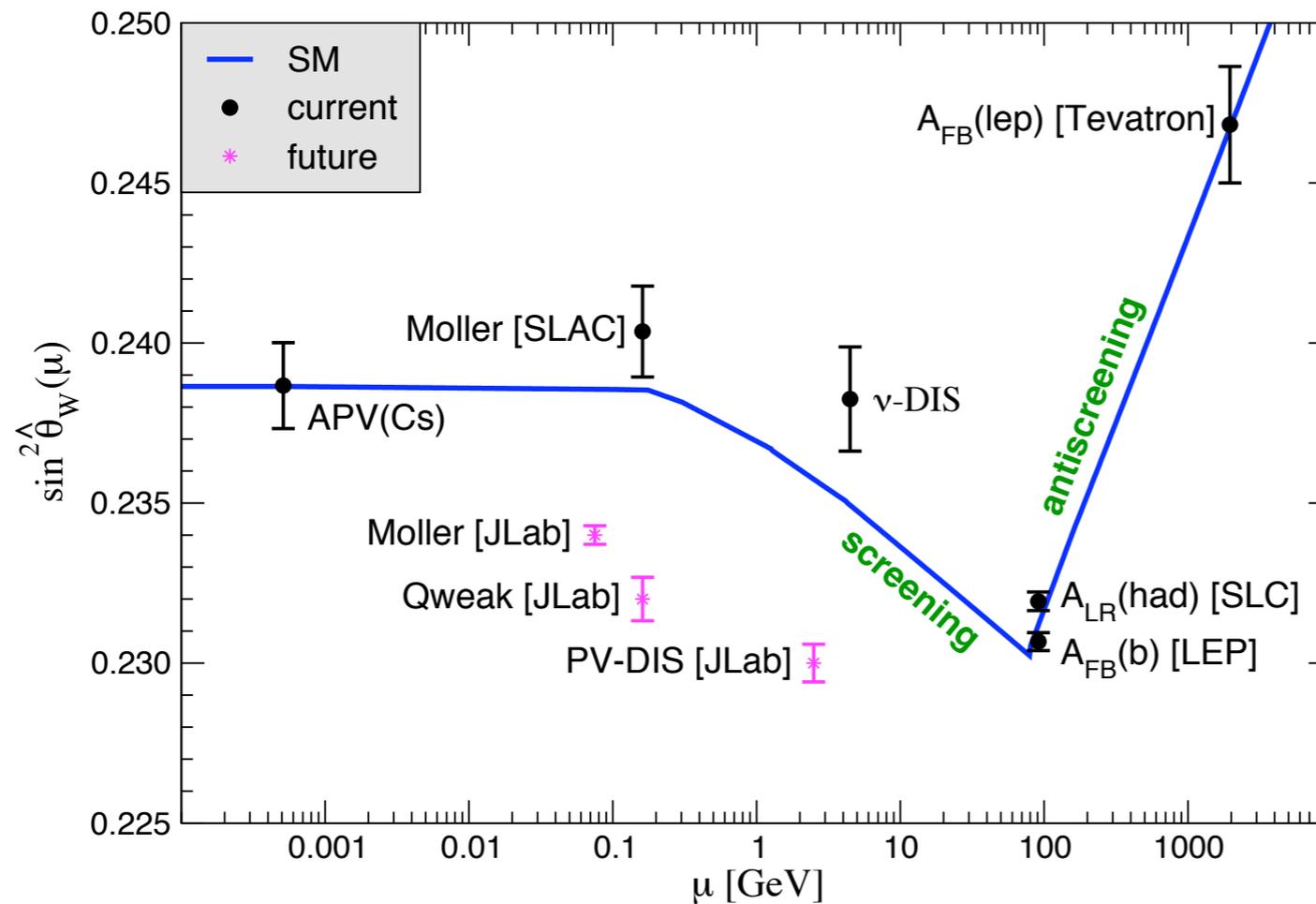
$$A_{\text{CG}}^{RL} = -\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \frac{9}{10} \left[\left(1 - \frac{20}{9} \sin^2 \theta_W\right) + (1 - 4 \sin^2 \theta_W) \frac{1 - (1 - y)^2}{1 + (1 - y)^2} \right]$$

All hadronic effects cancel!

Clean probe of
WNC

- Hadronic effects appear as small corrections to the CG formula.

Precision Era



(J. Erler, M. Ramsey-Musolf)

- 12 GeV program at JLab to begin 2014:
 - Moller
 - Qweak
 - SOLID, 6 GeV, and 12, GeV experiments
- The focus has shifted from the SM WNC theory to detecting hints of physics beyond the SM.

Corrections to Cahn-Gilman

- In the precision era, all corrections to CG must be under control

$$A_{RL} = -\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \frac{9}{10} \left[\tilde{a}_1 + \tilde{a}_2 \frac{1 - (1 - y)^2}{1 + (1 - y)^2} \right]$$

$$\tilde{a}_j = -\frac{2}{3} (2C_{ju} - C_{jd}) [1 + R_j(\text{new}) + R_j(\text{sea}) + R_j(\text{CSV}) + R_j(\text{TMC}) + R_j(\text{HT})]$$

↑
New physics

↑
Sea quarks

↑
Charge symmetry
violation

↑
Target mass

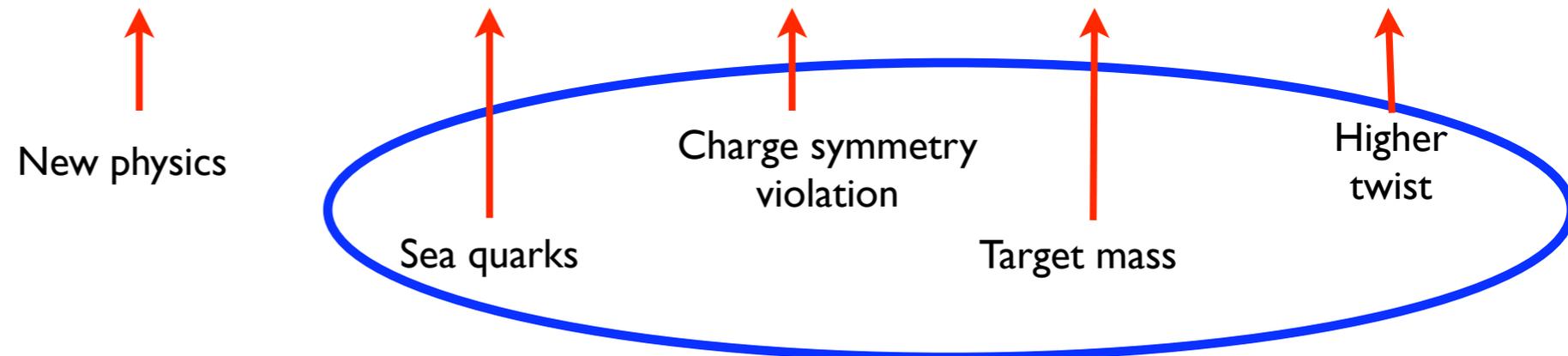
↑
Higher
twist

- Hadronic and electroweak effects must be well understood before any claim for evidence of new physics can be made.

Asymmetry as a Probe of Hadronic Physics

$$A_{RL} = -\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \frac{9}{10} \left[\tilde{a}_1 + \tilde{a}_2 \frac{1 - (1 - y)^2}{1 + (1 - y)^2} \right]$$

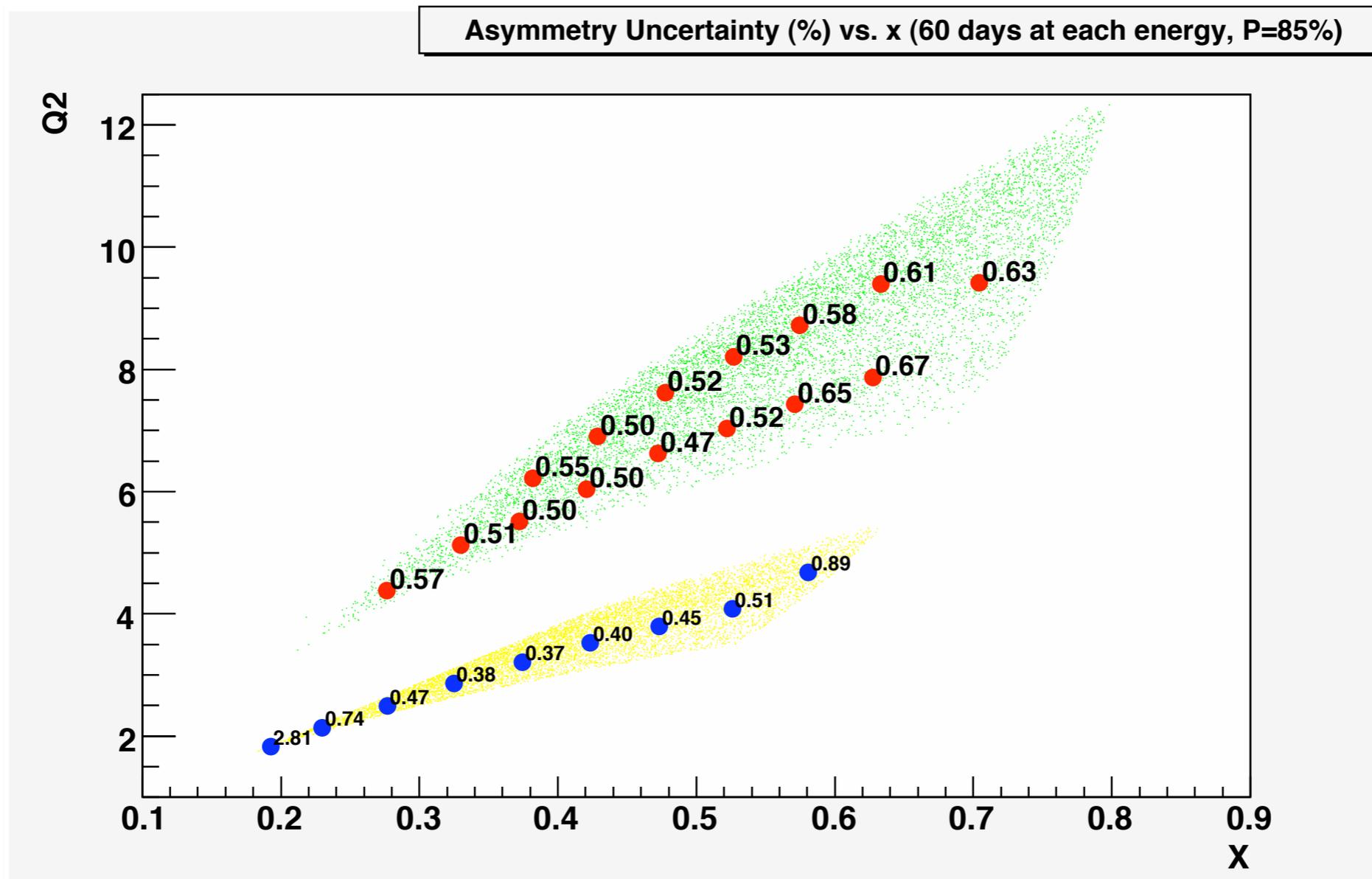
$$\tilde{a}_j = -\frac{2}{3} (2C_{ju} - C_{jd}) \left[1 + R_j(\text{new}) + R_j(\text{sea}) + R_j(\text{CSV}) + R_j(\text{TMC}) + R_j(\text{HT}) \right]$$



- Alternatively, precision PV DIS can be viewed as a probe of hadronic physics.
- Precision measurements over wide kinematic range can disentangle various effects.

SOLID

- SOLID plans to measure the asymmetry at a percent level over a wide kinematic range:



Projected data with errors for SOLID
(P. Souder)

Asymmetry as a Probe of Higher Twist

$$A_{RL} = -\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \frac{9}{10} \left[\tilde{a}_1 + \tilde{a}_2 \frac{1 - (1 - y)^2}{1 + (1 - y)^2} \right]$$

$$\tilde{a}_j = -\frac{2}{3} (2C_{ju} - C_{jd}) \left[1 + R_j(\text{new}) + R_j(\text{sea}) + R_j(\text{CSV}) + R_j(\text{TMC}) + R_j(\text{HT}) \right]$$

↑
New physics

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Sea quarks

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Charge symmetry
violation

↑
Target mass

↑
Higher
twist

- Precision PV DIS can be a probe of higher twist correlations.

Asymmetry as a Probe of Higher Twist

$$A_{RL} = -\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \frac{9}{10} \left[\tilde{a}_1 + \tilde{a}_2 \frac{1 - (1 - y)^2}{1 + (1 - y)^2} \right]$$

$$\tilde{a}_j = -\frac{2}{3} (2C_{ju} - C_{jd}) \left[1 + R_j(\text{new}) + R_j(\text{sea}) + R_j(\text{CSV}) + R_j(\text{TMC}) + R_j(\text{HT}) \right]$$

↑
New physics

↑
Sea quarks

↑
Charge symmetry
violation

↑
Target mass

↑
Higher
twist

- Precision PV DIS can be a probe of higher twist correlations.
- Higher twist effects in the first term of asymmetry is given by a single four-quark matrix element which probes quark-quark correlations. (Bjorken, Wolfenstein)

Some Definitions and Notation

- Asymmetry can be brought into the form:

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

- The Y_1 factor has the form:

$$Y_1 = \left(\frac{1 + R^{\gamma Z}}{1 + R^\gamma} \right) \frac{1 + (1 - y)^2 - y^2 \left[1 - r^2 / (1 + R^{\gamma Z}) \right] - 2xyM/E}{1 + (1 - y)^2 - y^2 \left[1 - r^2 / (1 + R^\gamma) \right] - 2xyM/E}$$

- The Y_3 factor has the form:

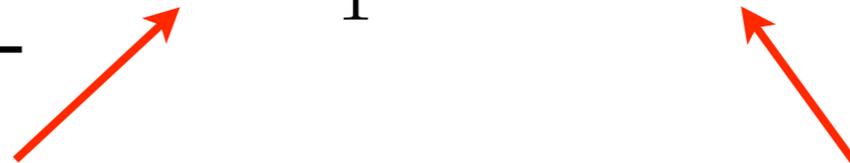
$$Y_3 = \left(\frac{r^2}{1 + R^\gamma} \right) \frac{1 - (1 - y)^2}{1 + (1 - y)^2 - y^2 \left[1 - r^2 / (1 + R^\gamma) \right] - 2xyM/E}$$

- We have used the definitions:

$$R^{\gamma(\gamma Z)} \equiv \frac{\sigma_L^{\gamma(\gamma Z)}}{\sigma_T^{\gamma(\gamma Z)}} = r^2 \frac{F_2^{\gamma(\gamma Z)}}{2x F_1^{\gamma(\gamma Z)}} - 1, \quad r^2 = 1 + \frac{4M^2 x^2}{Q^2}$$

Key features of the Asymmetry Terms

- Asymmetry can be brought into the form:

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$


- Dominant term in asymmetry
- Can in principle be kinematically distinguished from second term (independent of y)
- Can be sensitive to only quark-quark correlations
- A single twist-4 matrix element determines quark-quark correlations.
- suppressed by small electron vector coupling
- Can be kinematically distinguished from second term (dependent on y)
- Can be sensitive to quark-quark and quark-gluon correlations
- Multiple twist-4 matrix elements determine correlations
- Can be extracted from neutrino scattering data

Key features of the Asymmetry Terms

- Asymmetry can be brought into the form: Focus of this talk

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

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Cahn-Gilman Limit

- Cahn-Gilman limit:

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

$$R^\gamma = R^{\gamma Z} = r^2 - 1,$$
$$Y_1 = 1$$

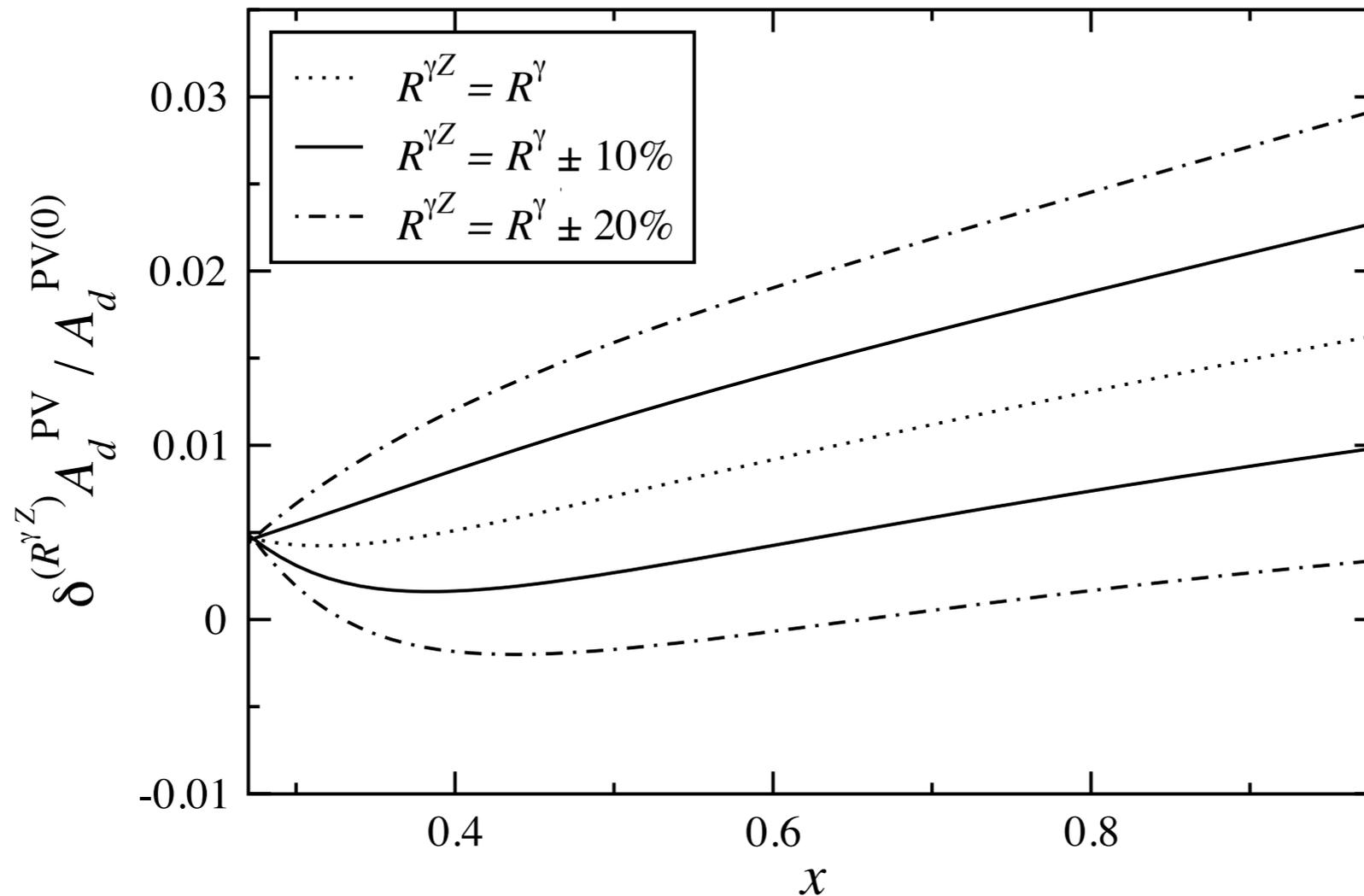
$$\left[\frac{F_1^{\gamma Z}}{F_1^\gamma} \right]_{\text{CG}} = \frac{9}{10} \left(1 - \frac{20}{9} \sin^2 \theta_W \right)$$

- Higher twist effects can modify these relations.

Hobbs/Melnitchouck Analysis

- Considered the possibility that twist-4 effects arise entirely through the relation:

$$R^\gamma \neq R^{\gamma Z}$$



- Concluded that:
 - 20% difference gives a 1% effect in asymmetry
 - Could interfere with extraction of CSV effects

More Recent Analysis

(SM, M.Ramsey-Musolf, G.Sacco)

- Our conclusions based on the Bjorken/Wolfenstein argument:
 - Twist-4 effects in vector WNC term come only from quark-quark correlations.
 - A single 4-quark twist-4 matrix element contributes to the vector WNC term.
 - The relation $R^{\gamma Z} = R^{\gamma}$ holds true at twist-4 up to perturbative corrections.

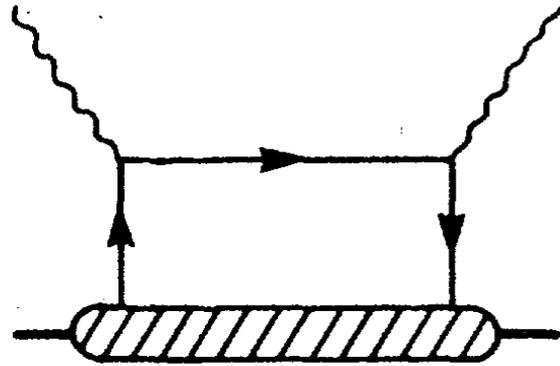
Only quark-quark
correlations given by
a single matrix element

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^{\gamma}} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^{\gamma}} \right]$$

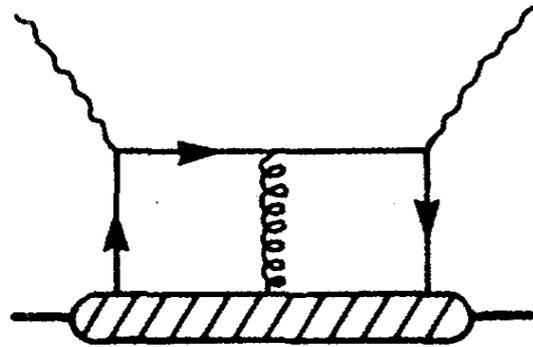
$$Y_1 = 1$$

Twist-4 effects
reside in ratio
of form factors

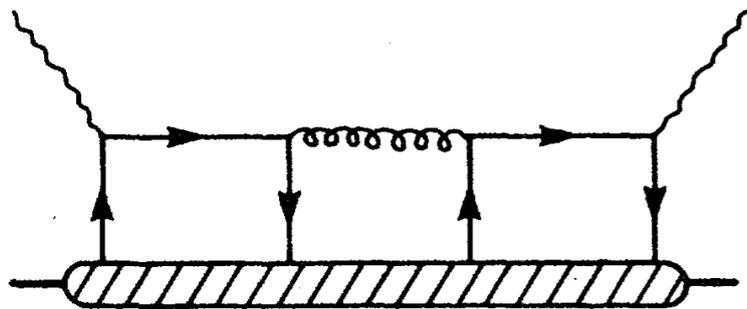
Operator Product Expansion



Twist-2



Quark-gluon correlation (Twist-2 + Twist-4)



Quark-quark correlation (Twist-4)



$$\mathcal{O}_{ud}^{\mu\nu}(x) = \frac{1}{2} [\bar{u}(x) \gamma^\mu u(x) d(0) \gamma^\nu d(0) + (u \leftrightarrow d)]$$

Bjorken-Wolfenstein Argument

- Isospin decomposition of electromagnetic and vector neutral currents:

$$J_{\gamma}^{\mu} = v_{\mu} + \frac{1}{3}s_{\mu} - \frac{1}{3}\lambda_{\mu}, \quad J_Z^{V\mu} = 2\left[(1 - 2\sin^2\theta)v_{\mu} - \frac{2}{3}\sin^2\theta s_{\mu} - \left(\frac{1}{2} - \frac{2}{3}\sin^2\theta\right)\lambda_{\mu}\right]$$

$$v_{\mu} = \frac{1}{2}(\bar{u}\gamma_{\mu}u - \bar{d}\gamma_{\mu}d), \quad s_{\mu} = \frac{1}{2}(\bar{u}\gamma_{\mu}u + \bar{d}\gamma_{\mu}d), \quad \lambda_{\mu} = \bar{s}\gamma_{\mu}s$$

- Isospin decomposition of electromagnetic and interference hadronic tensors

$$W_{\mu\nu}^{\gamma} = W_{\mu\nu}^{vv} + \frac{1}{9}W_{\mu\nu}^{ss}.$$

$$W_{\mu\nu}^{V;\gamma Z} = 2(1 - 2\sin^2\theta)W_{\mu\nu}^{vv} - \frac{4}{9}\sin^2\theta W_{\mu\nu}^{ss}$$

Bjorken-Wolfenstein Argument

- Isospin decomposed hadronic tensors:

$$W_{\mu\nu}^{vv} = \frac{1}{2\pi M} \int d^4x e^{iq\cdot x} \langle D(P) | v_\mu(x) v_\nu(0) | D(P) \rangle$$
$$W_{\mu\nu}^{ss} = \frac{1}{2\pi M} \int d^4x e^{iq\cdot x} \langle D(P) | s_\mu(x) s_\nu(0) | D(P) \rangle$$

- Twist-4 quark-quark correlation hadronic tensor:

$$W_{\mu\nu}^{du} = W_{\mu\nu}^{ss} - W_{\mu\nu}^{vv},$$
$$= \frac{1}{2\pi M} \int d^4x e^{iq\cdot x} \langle D(P) | \frac{1}{2} \{ \bar{d}(x) \gamma_\mu d(x) \bar{u}(0) \gamma_\nu u(0) + (u \leftrightarrow d) \} | D(P) \rangle$$

Bjorken-Wolfenstein Argument

- Isospin decomposed hadronic tensors:

$$W_{\mu\nu}^{vv} = \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | v_\mu(x) v_\nu(0) | D(P) \rangle$$

$$W_{\mu\nu}^{ss} = \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | s_\mu(x) s_\nu(0) | D(P) \rangle$$

- Twist-4 quark-quark correlation hadronic tensor:

$$W_{\mu\nu}^{du} = W_{\mu\nu}^{ss} - W_{\mu\nu}^{vv},$$

$$= \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | \frac{1}{2} \{ \bar{d}(x) \gamma_\mu d(x) \bar{u}(0) \gamma_\nu u(0) + (u \leftrightarrow d) \} | D(P) \rangle$$

- Structure Function definitions

$$W_{\mu\nu}^{vv,ss,du} = \left(-g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} \right) \frac{F_1^{vv,ss,du}}{M} + \left(P_\mu - \frac{P \cdot q}{q^2} q_\mu \right) \left(P_\nu - \frac{P \cdot q}{q^2} q_\nu \right) \frac{F_2^{vv,ss,du}}{M P \cdot q}$$

Bjorken-Wolfenstein Argument

- Isospin decomposed hadronic tensors:

$$W_{\mu\nu}^{vv} = \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | v_\mu(x) v_\nu(0) | D(P) \rangle$$

$$W_{\mu\nu}^{ss} = \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | s_\mu(x) s_\nu(0) | D(P) \rangle$$

- Twist-4 quark-quark correlation hadronic tensor:

$$W_{\mu\nu}^{du} = W_{\mu\nu}^{ss} - W_{\mu\nu}^{vv},$$

$$= \frac{1}{2\pi M} \int d^4x e^{iq \cdot x} \langle D(P) | \frac{1}{2} \{ \bar{d}(x) \gamma_\mu d(x) \bar{u}(0) \gamma_\nu u(0) + (u \leftrightarrow d) \} | D(P) \rangle$$

- Structure Function definitions

$$W_{\mu\nu}^{vv,ss,du} = \left(-g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} \right) \frac{F_1^{vv,ss,du}}{M} + \left(P_\mu - \frac{P \cdot q}{q^2} q_\mu \right) \left(P_\nu - \frac{P \cdot q}{q^2} q_\nu \right) \frac{F_2^{vv,ss,du}}{M P \cdot q}$$

$$F_{1,2}^{vv} = F_{1,2}^{ss} - F_{1,2}^{du}$$

Bjorken-Wolfenstein Argument

- Original structure functions can be written as:

$$F_{1,2}^{\gamma} = \frac{10}{9} F_{1,2}^{ss} - F_{1,2}^{du}$$

$$F_{1,2}^{\gamma Z} = 2\left(1 - \frac{20}{9} \sin^2 \theta\right) F_{1,2}^{ss} - 2\left(1 - 2 \sin^2 \theta\right) F_{1,2}^{du}$$

- Asymmetry in terms of original structure functions:

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^{\gamma}} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^{\gamma}} \right]$$



- YI term:

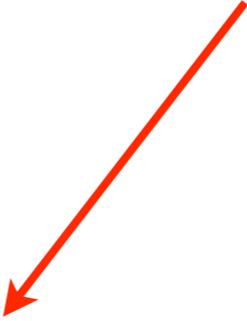
$$A_{RL}^V = -\frac{9}{10} \left(\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \right) g_A^e \left\{ \left(1 - \frac{20}{9} \sin^2 \theta \right) - \frac{1}{10} \frac{F_1^{du}}{F_{1;LT}^{ss}} + \dots \right\}$$

Form of twist-4 correction

- YI term:

$$A_{RL}^V = -\frac{9}{10} \left(\frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \right) g_A^e \left\{ \left(1 - \frac{20}{9} \sin^2 \theta \right) - \frac{1}{10} \frac{F_1^{du}}{F_{1;LT}^{ss}} + \dots \right\}$$

- Twist-4 correction given by:

$$R_1(\text{HT}) = \left[\frac{-4}{5 \left(1 - \frac{20}{9} \sin^2 \theta_W \right)} \right] \frac{F_1^{du}}{u_p(x) + d_p(x)}.$$


$$R^{\gamma Z} = R^{\gamma}$$

- Quark-quark correlation twist-4 operator matrix element:

twist-4 structure functions



$$\frac{1 + R^{\gamma Z}}{1 + R^{\gamma}} = 1 + \frac{(F_2^{du} - 2x F_1^{du})}{2x F_{1;LT}^{ss}} \left[\frac{9}{10} - \frac{1 - 2 \sin^2 \theta}{1 - \frac{20}{9} \sin^2 \theta} \right]$$

↑
twist-2 structure function

- Using the Callan-Gross relation at tree level we get:

$$F_2^{du} = 2x F_1^{du} \longrightarrow \frac{1 + R^{\gamma Z}}{1 + R^{\gamma}} = 1$$

(R.Ellis, W.Furmanski, R.Petronzio; X.Ji; J.Qiu)

- We also give an effective field theory (SCET) argument (SM, M. Ramsey-Musolf, G.Sacco)

$$R^{\gamma Z} = R^{\gamma}$$

$$\frac{1 + R^{\gamma Z}}{1 + R^{\gamma}} = 1$$

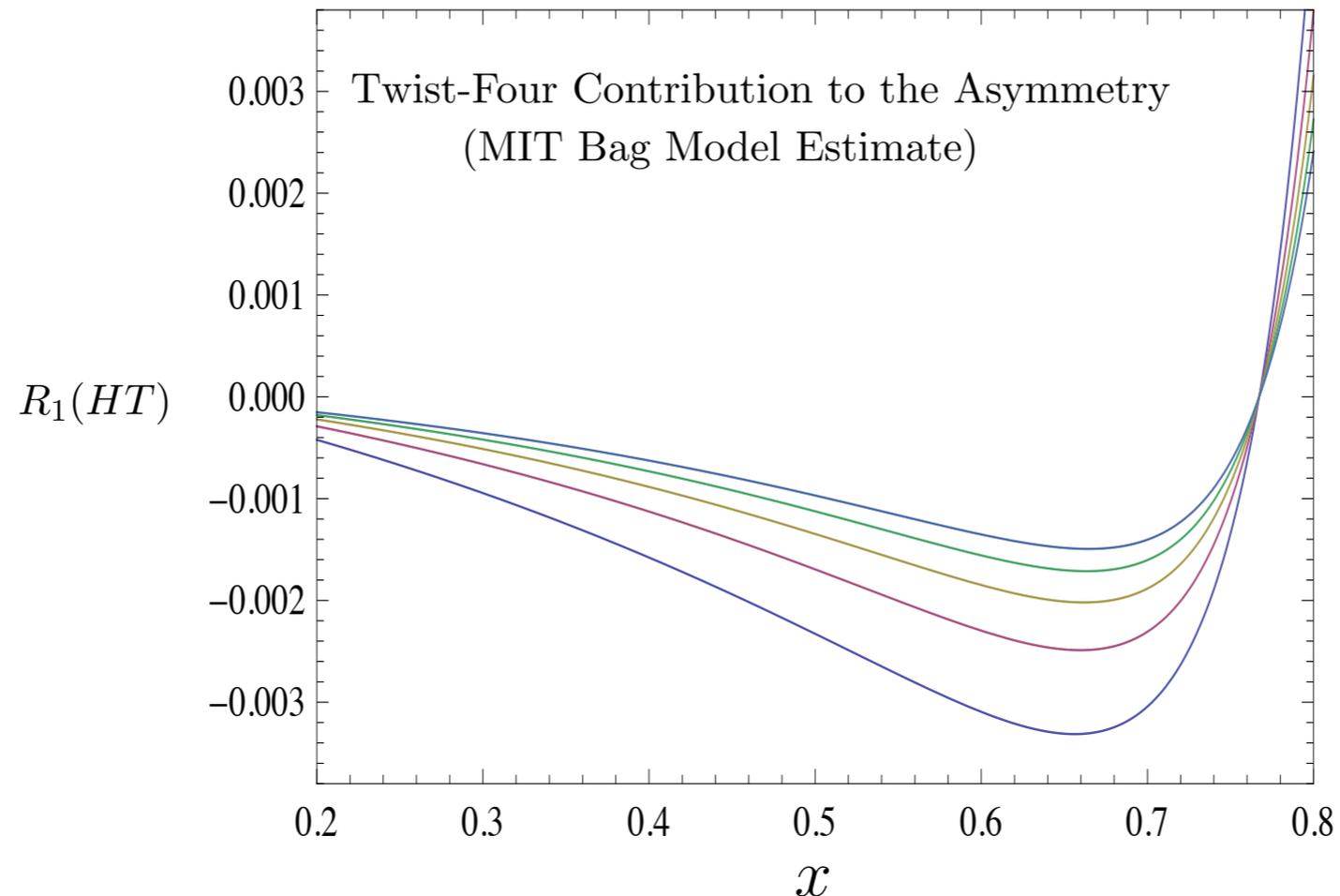
- Using the Callan-Gross relation at tree level we get:

$$A_{RL} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^{\gamma}} + g_V^e Y_3 \frac{F_3^{\gamma Z}}{F_1^{\gamma}} \right]$$

free of twist-4 effects

twist-4 quark-quark correlations
reside in ratio of structure
functions

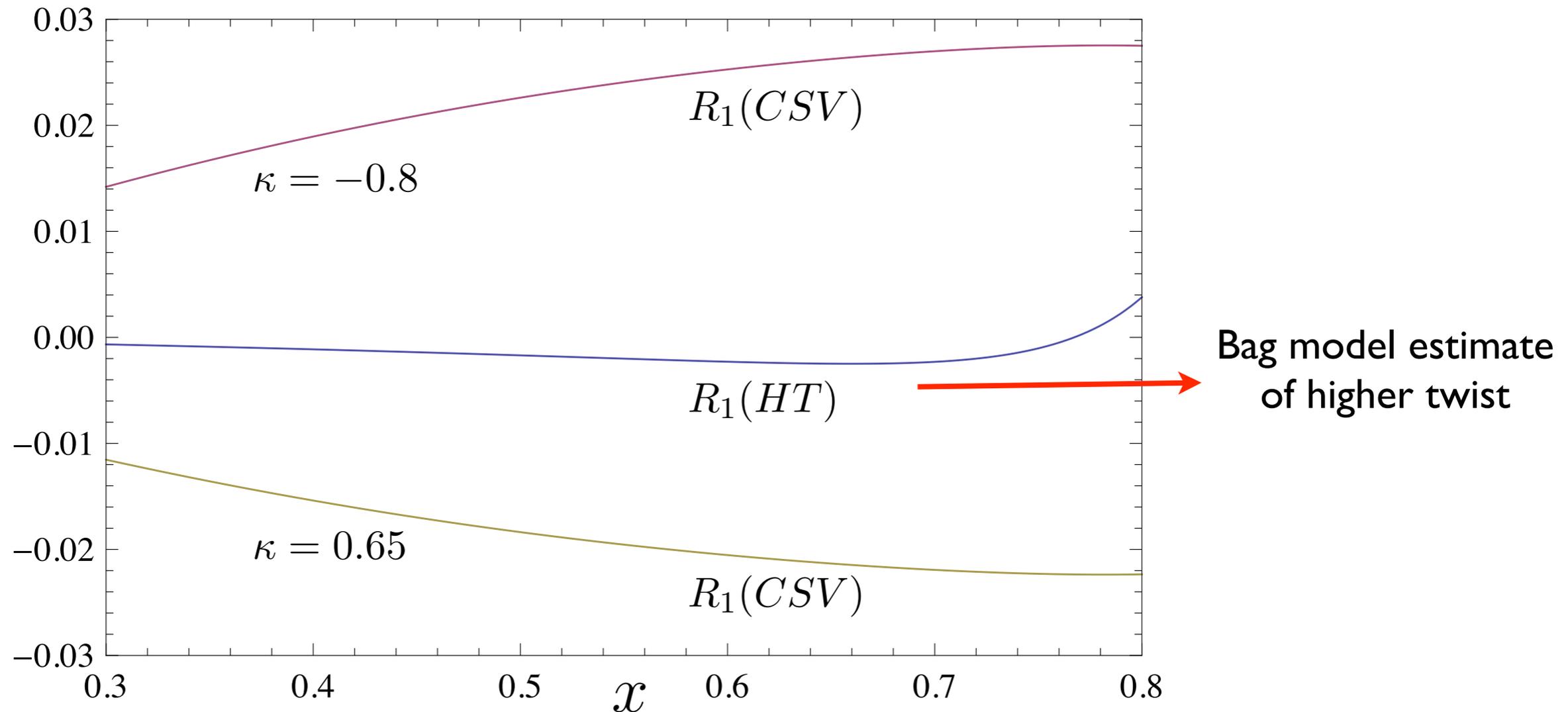
Form of twist-4 correction



$$R_1(HT) = \left[\frac{-4}{5\left(1 - \frac{20}{9} \sin^2 \theta_W\right)} \right] \frac{F_1^{du}}{u_p(x) + d_p(x)}.$$

- Bag model estimate of quark-quark correlation is below the half-percent level.
- If the Bag Model estimate is accurate, then higher twist physics becomes difficult to extract.

CSV vs Higher Twist



$$\delta u - \delta d = 2\kappa f(x), \quad f(x) = x^{-1/2}(1-x)^4(x - 0.0909)$$

- Negligible higher twist effects can allow for a cleaner extraction of CSV or new physics effects.

Conclusions

- PV DIS can be a powerful probe of hadronic physics beyond the parton model.
- The precision and wide kinematic reach of SOLID can in principle disentangle various hadronic effects such as sea quarks, CSV, and higher twist.
- PV DIS can probe a 'single' twist-4 quark-quark correlation matrix element and is the only known observable with this property.
- Uncertainties in $R\text{-}\gamma\text{-}Z$ will have a much smaller effect in the separation of higher twist and CSV effects than previously thought.